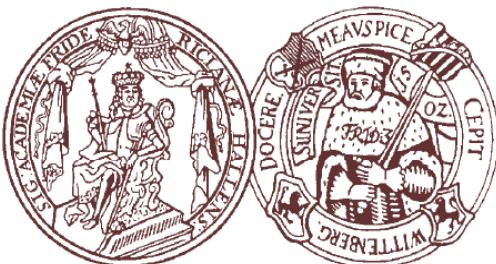


Verifying the RTE model - ortho-positronium lifetime measurement on controlled pore glasses



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D. Enke², R. Krause-Rehberg¹

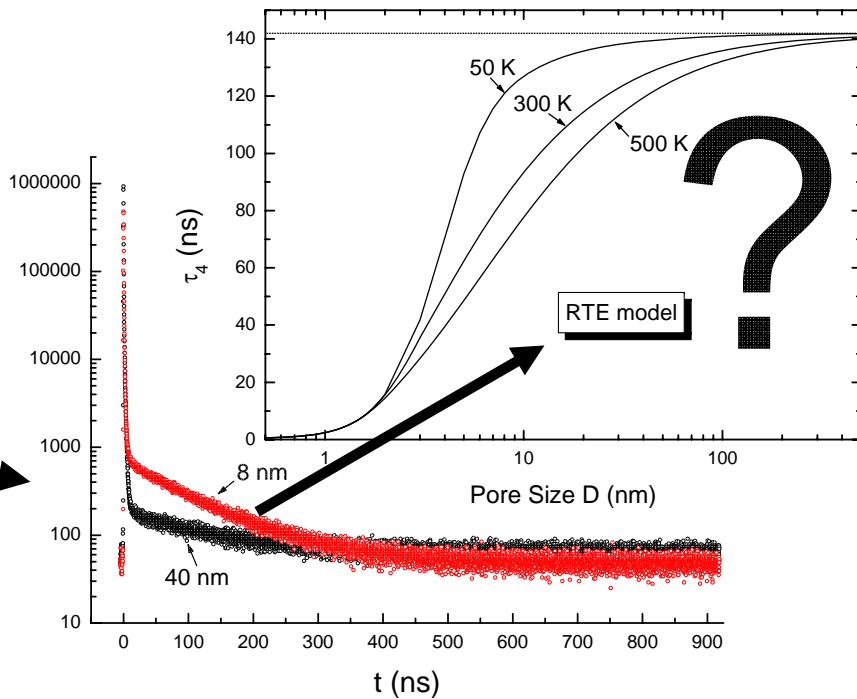
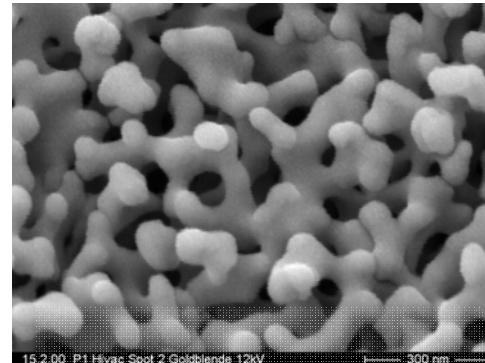
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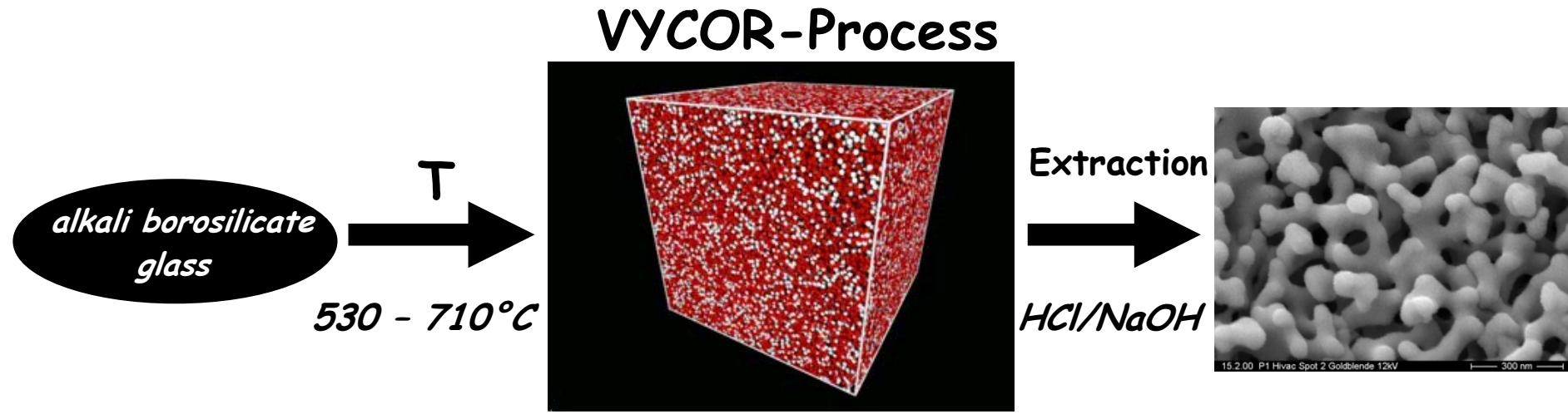
²Department of Chemistry

Verifying the RTE model

- Porous glass
- Models - the state of the art
- Experimental results
- Summary



Controlled pore glasses - CPG



d_p 1 to 110 nm

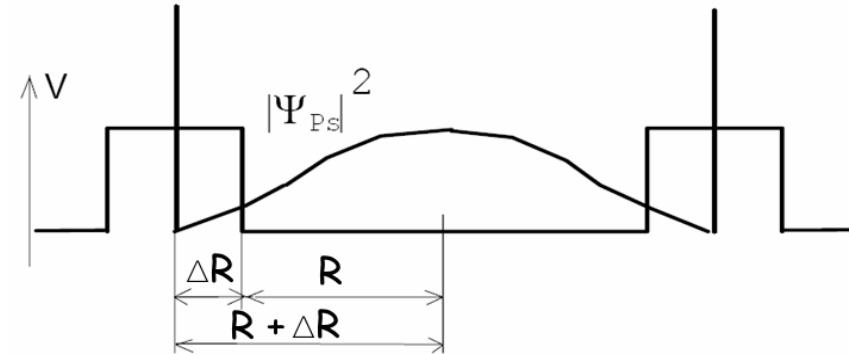
- spinodal phase separation
- decomposition is initiated by heat treatment
- alkali rich borate phase \leftrightarrow pure silica
- alkali phase soluble in acid \rightarrow silica network
- pore size depends on basic material
- shape depends on duration and T of heat treatment

The TE model

- Annihilation rate: $\frac{1}{\tau_{o-Ps}} = \lambda_{o-Ps}$
 $= \lambda_{2\gamma} + \lambda_{3\gamma}$
 $= \lambda_{2\gamma}^0(P) + \lambda_{3\gamma}^0(1-P) \cong \lambda_{2\gamma}^0(P)$

$$\lambda_{2\gamma}^0 = \frac{\lambda_s + 3\lambda_T}{4} = \lambda_A \approx 2ns^{-1}$$

- Pore size < 1 nm $\rightarrow \lambda_{3\gamma}$ neglected, only pick off annihilation



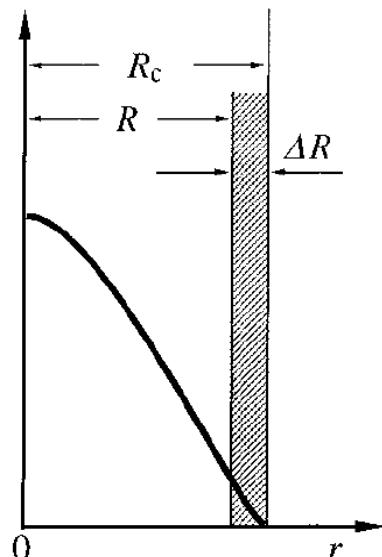
$$\lambda_{TE}(R) = \lambda_A \left[1 - \frac{R}{R + \Delta R} + \frac{1}{2\pi} \sin\left(\frac{2\pi R}{R + \Delta R}\right) \right]$$

- $\Delta R = 0.166$ nm determined by Eldrup
- Pore size > 1 nm $\rightarrow \lambda_{3\gamma}$ can not be neglected, temperature dependence of o-Ps lifetime (excited states)

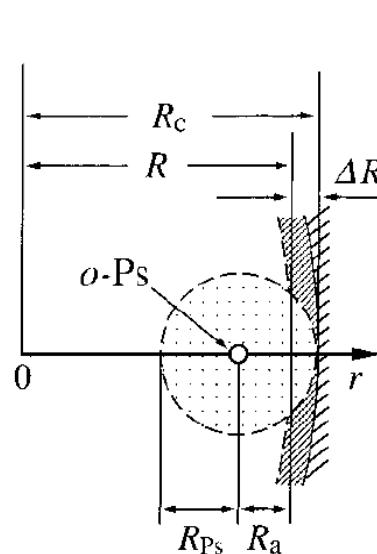
The 2 models for $R > 1 \text{ nm}$ - Tokyo

- Tokyo model:** $\lambda_{Tokyo}(R) = \begin{cases} \lambda_{TE} + \lambda_{3\gamma} & (R < R_a) \\ \lambda_{TE}(R_a) \left[1 - \left(\frac{R - R_a}{R + \Delta R} \right)^b \right] + \lambda_{3\gamma} & (R \geq R_a) \end{cases}$

- Problems:**
 - no explicit temperature dependence
 - two free parameters to be determined



(a) TE



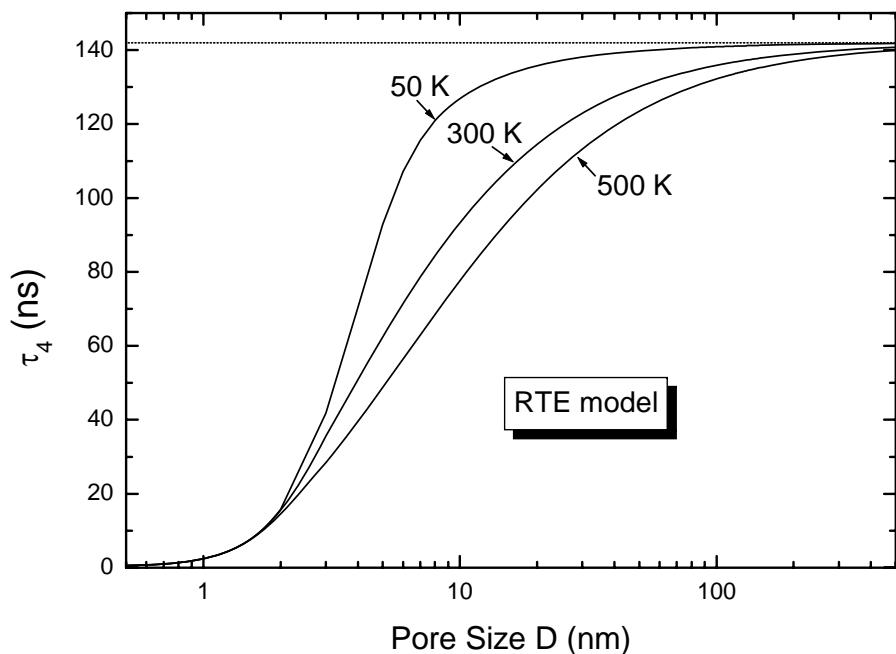
(b) Tokyo

empirical:
 $R_a = 0.8 \text{ nm}$
 $b = 0.55$

The 2 models for $R > 1 \text{ nm}$ - RTE

- RTE model (for 3D cubic pores):

$$\lambda_{RTE}(D, T) = \lambda_A - \frac{\lambda_s - \lambda_{3\gamma}}{4} \left[1 - \frac{2\delta}{D} + \frac{\sum_{i=1}^{\infty} \frac{1}{i\pi} \sin\left(\frac{2i\pi\delta}{D}\right) e^{\left(\frac{-\beta i^2}{D^2 kT}\right)}}{\sum_{i=1}^{\infty} e^{\left(\frac{-\beta i^2}{D^2 kT}\right)}} \right]^3$$



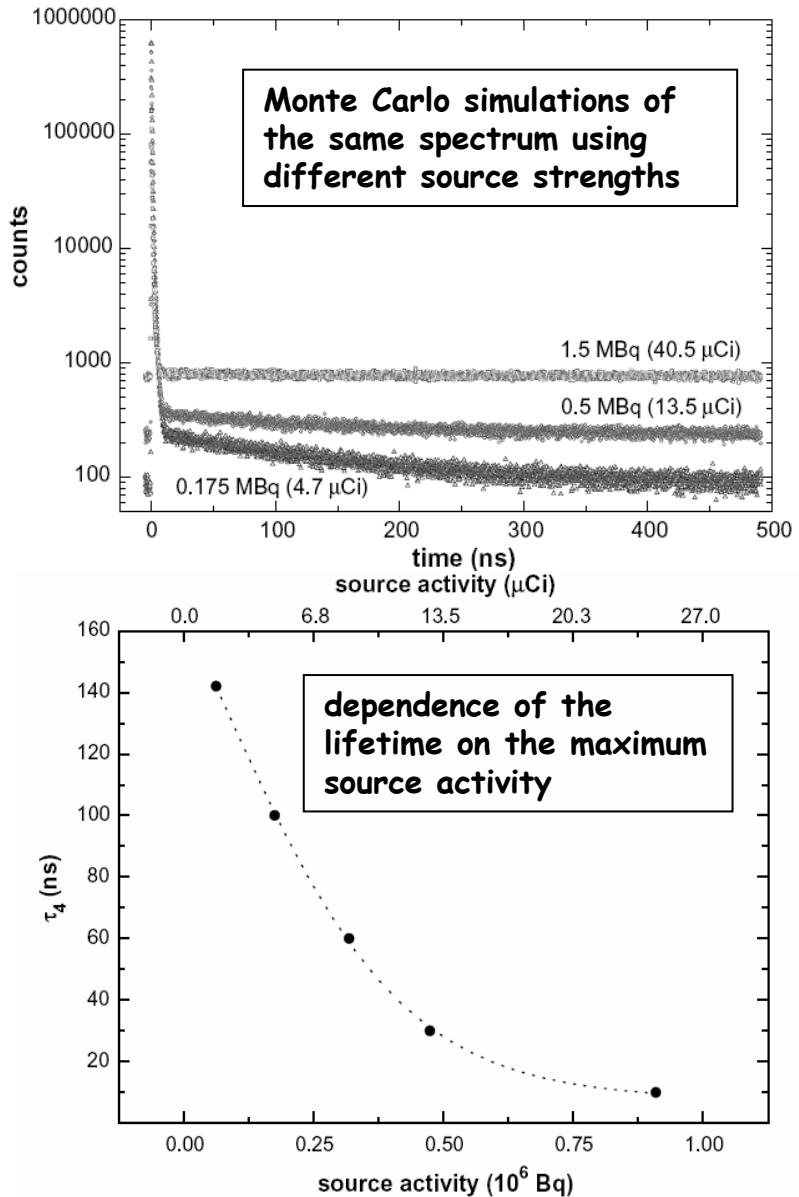
- Boltzmann statistics ascribes explicit temperature dependence to the lifetime
- Rectangular geometry \rightarrow prevention of complicated Bessel functions
- $\delta = 0.18 \text{ nm}$ analogous to TE model

D. W. Gidley, T. L. Dull, W. E. Frieze, J. N. Sun, A. F. Yee, *J. Phys. Chem. B* 2001, 105, 4657.

Verifying the RTE model

The experiments

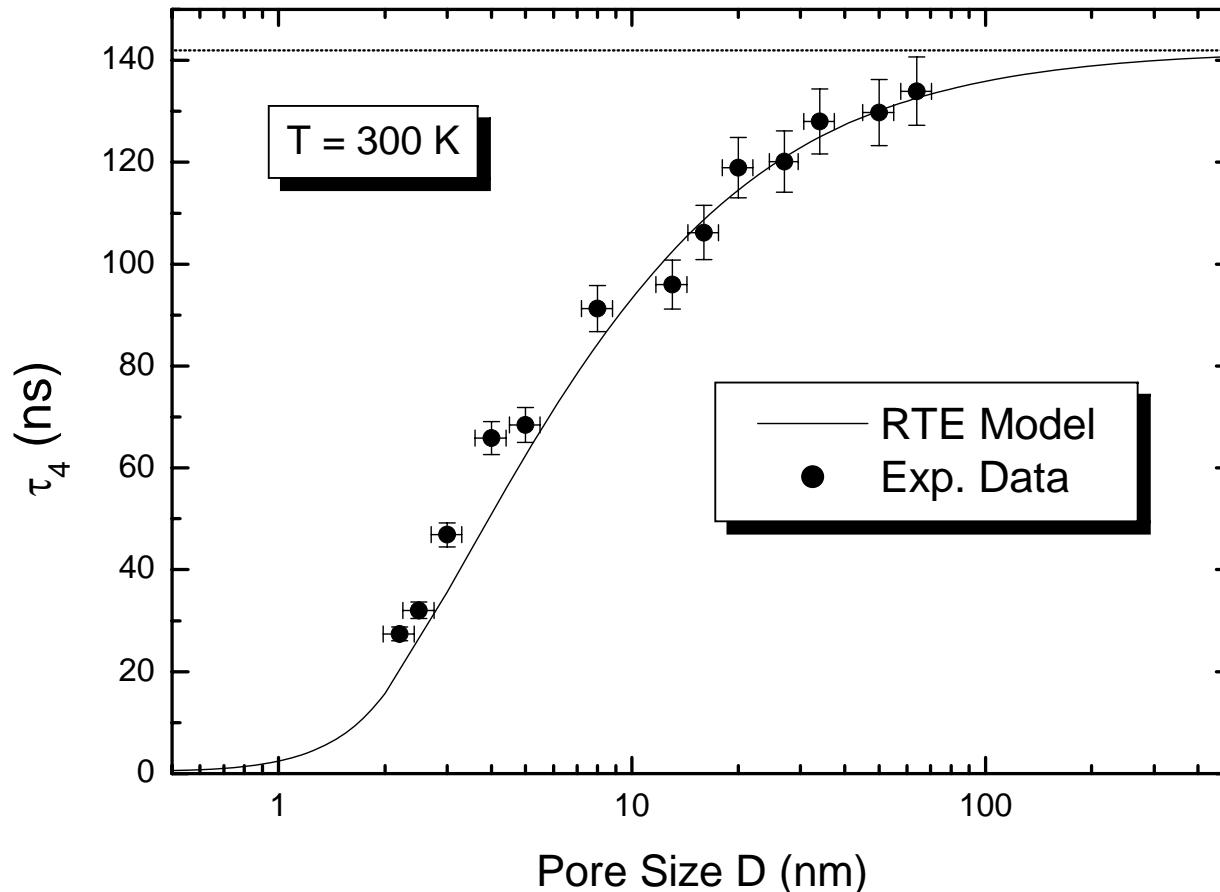
- Important: weak source required to obtain o-Ps lifetime properly (long lifetime component disturbed by chance coincidences)
- When expecting a lifetime of e.g. 120 ns \rightarrow max. source strength of 3 μCi recommended
- At first measurements at $T = 300 \text{ K}$ on different pore sizes



S. Thraenert, E.M. Hassan, R. Krause-Rehberg, *Nucl. Instrum. and Meth. B* 2006, Vol. 248 No. 2, 336.

Verifying the RTE model

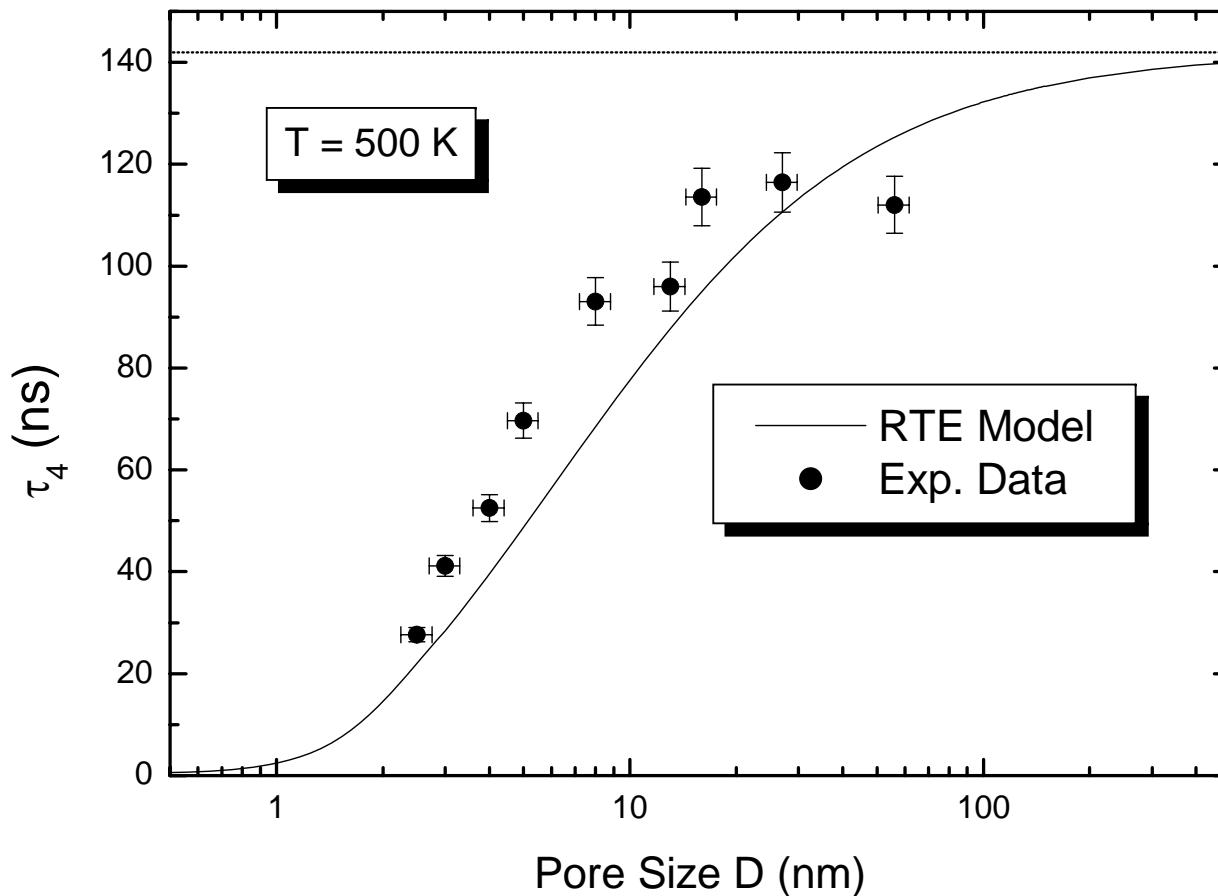
The experiments at $T = 300 \text{ K}$



- for $T = 300 \text{ K}$ general agreement to the RTE model
- calibration curve for the correlation of o-Ps lifetime and pore size

Verifying the RTE model

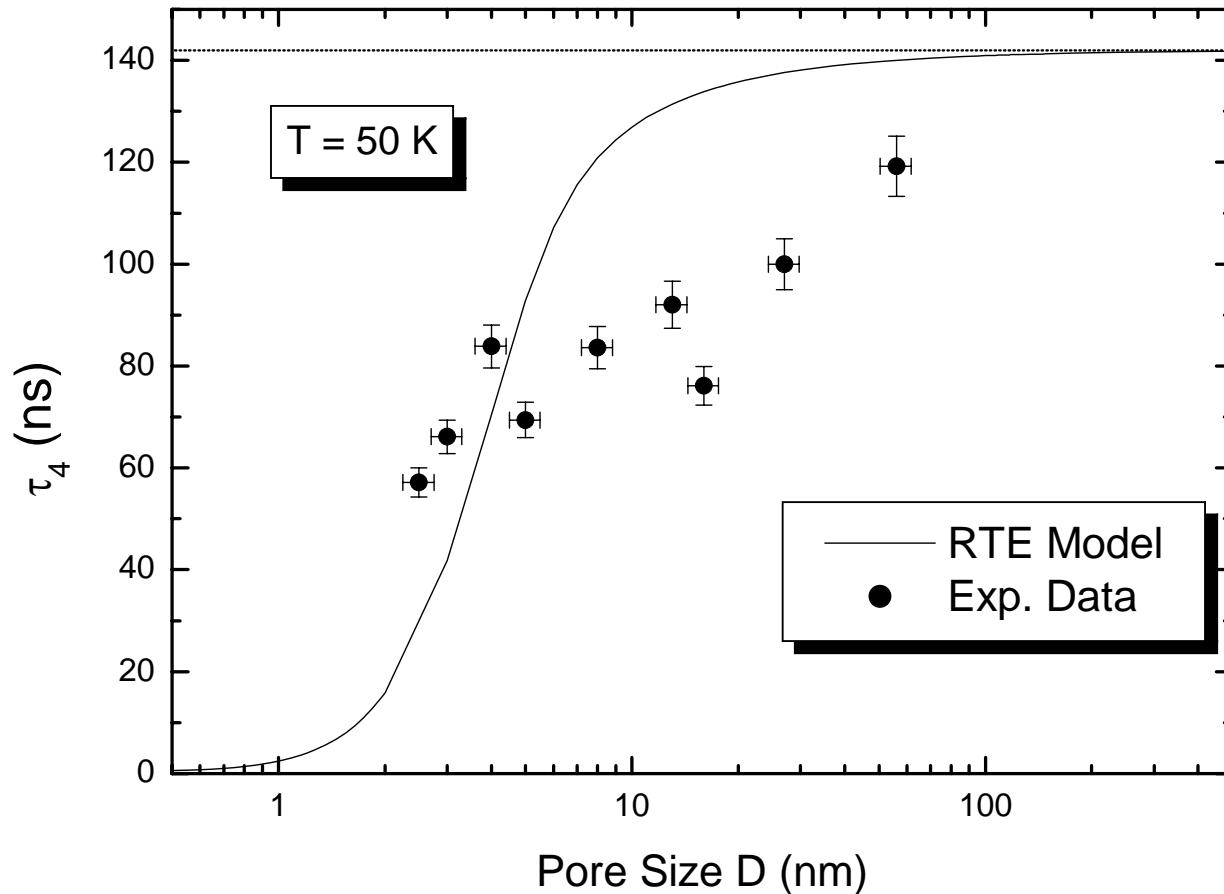
The experiments at $T = 500$ K



- for $T = 500$ K still acceptable agreement to the RTE model

Verifying the RTE model

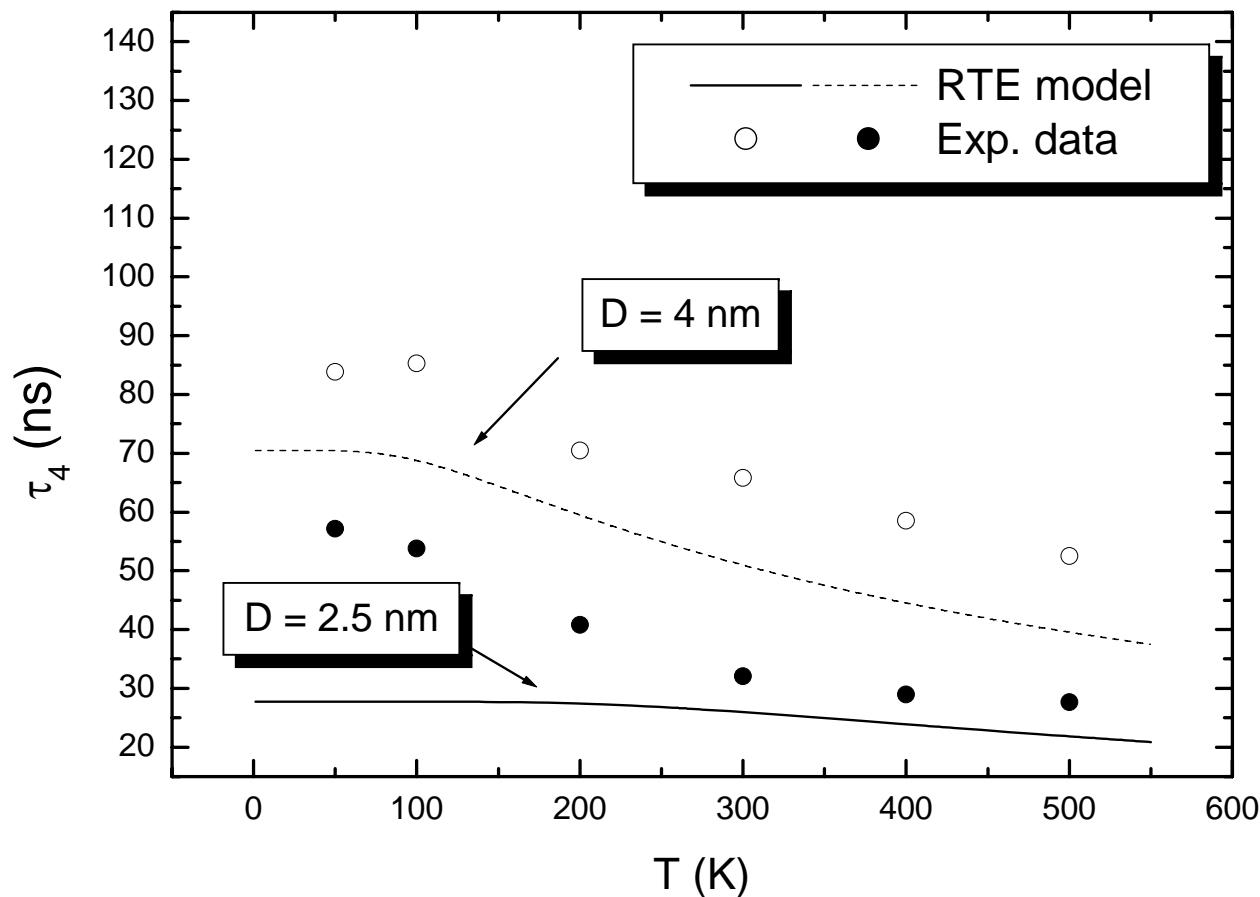
The experiments at $T = 50$ K



- for $T = 50$ K no agreement to the RTE model can be observed

Verifying the RTE model

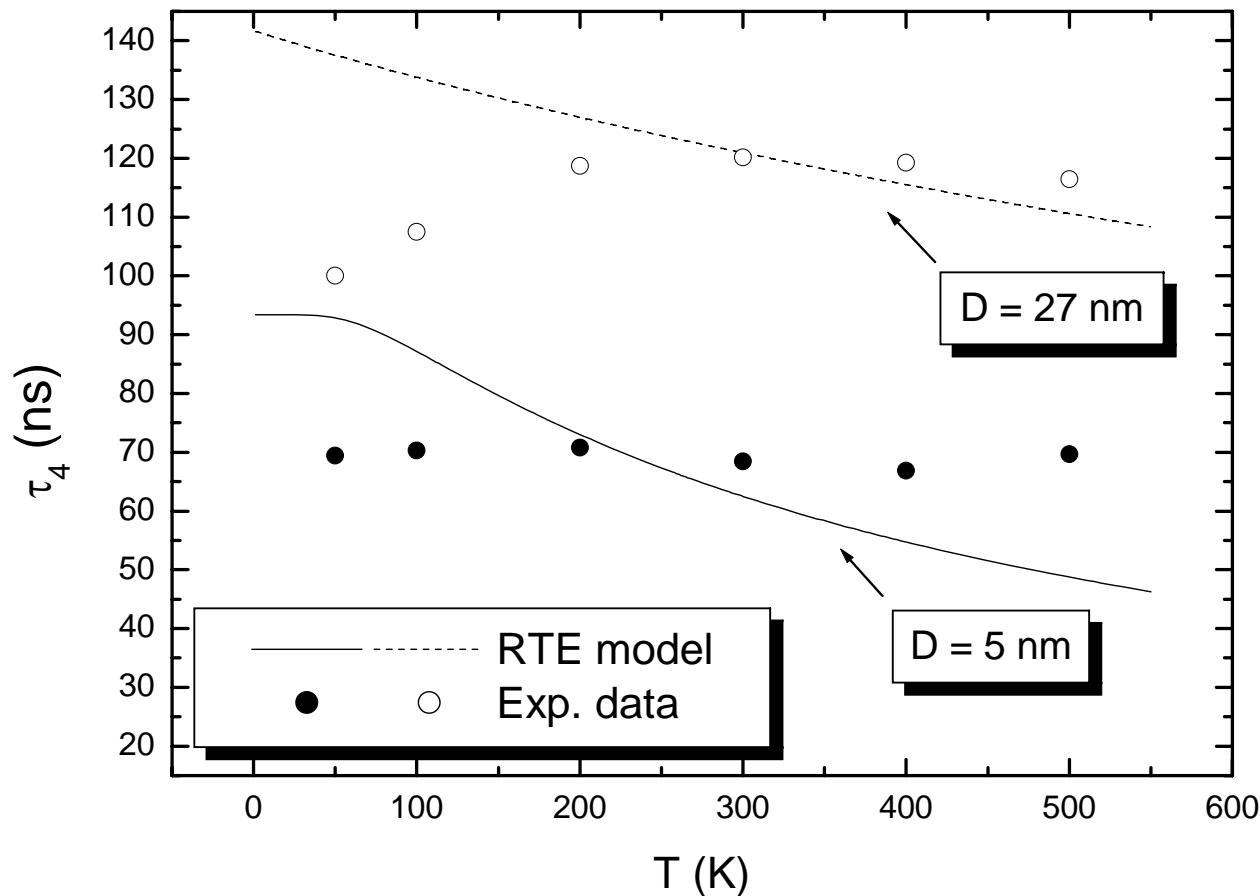
The temperature dependence



- for $D = 2.5 \text{ nm}$ poor agreement to RTE model for $T < 300 \text{ K}$
- for $D = 4 \text{ nm}$ shape of exp. data like RTE model

Verifying the RTE model

The temperature dependence

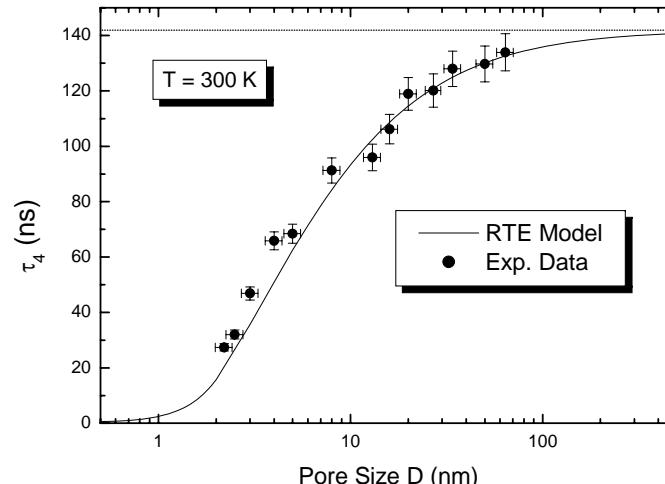
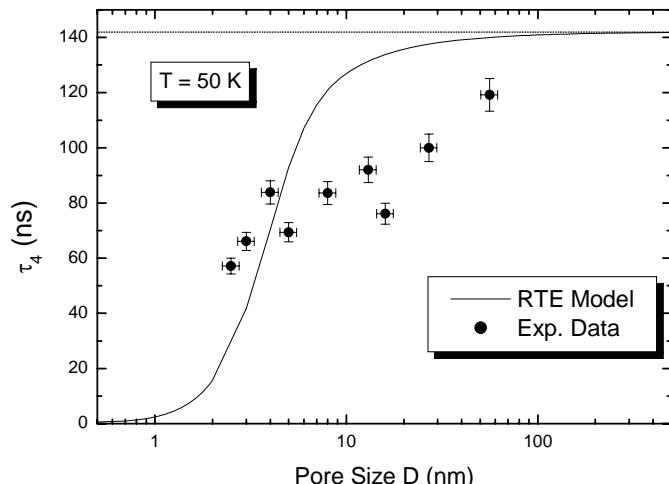


- for $D = 5 \text{ nm}$ no temperature dependence to observe
- for $D = 27 \text{ nm}$ contrary behaviour to the RTE model

Verifying the RTE model

Summary

- for $T = 300$ K general agreement to the RTE model \rightarrow at room temperature, PALS is a useful porosimetry tool!
- for $T > 300$ K still agreement to the RTE model.
- for low temperatures the measurements show disagreement to the RTE model



Verifying the RTE model

Summary - temperature dependence

- for small pores ($D < 3 \text{ nm}$) the lifetime increases at low temperatures
- for $D = 4 \text{ nm}$ temperature dependence of lifetime fairly agrees to the RTE model
- for $D = 5 \text{ nm}$ no temperature dependence of the lifetime can be observed
- for large Pores ($D > 8 \text{ nm}$) the lifetime decreases at low temperatures -> contrary behaviour to the model.

- Thanks for your patience!
- This talk as pdf?

■ <http://positron.physik.uni-halle.de>