

# Nano-scale porosimetry using ortho-Positronium lifetime measurement

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# Outline

## ■ Principles of PALS

- positron and positronium
- lifetime measurement
- the spectrum

## ■ Porous glass - CPG

- synthesis
- properties

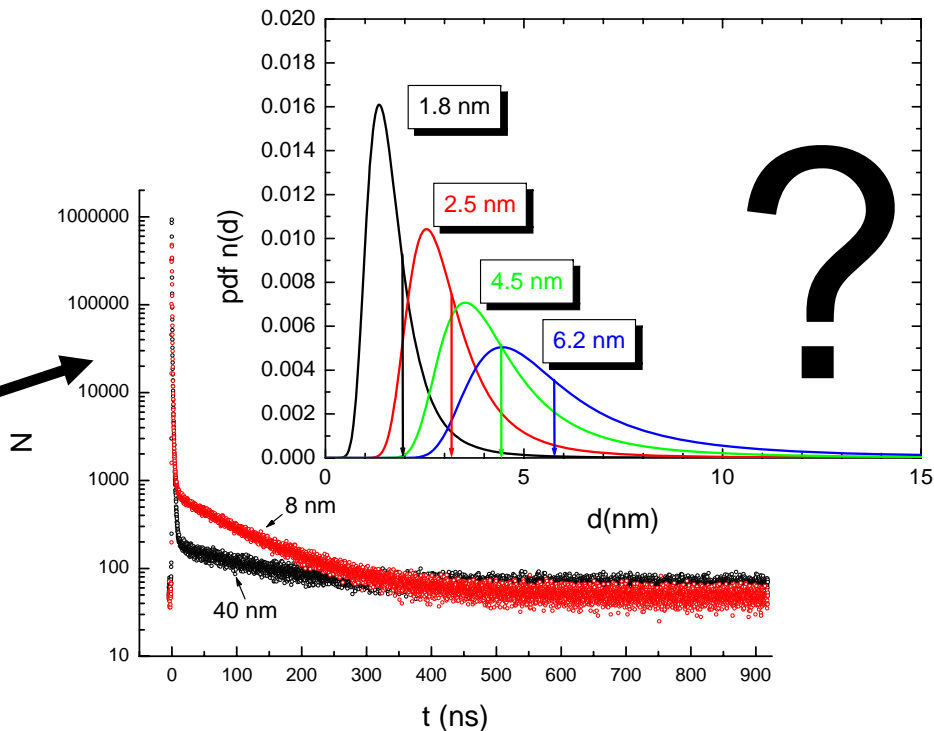
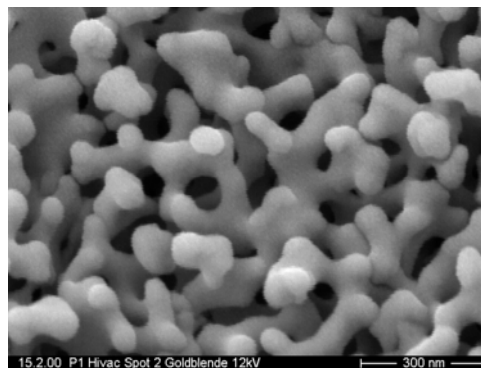
## ■ From $\tau_4$ to pore size $d$

- the model

## ■ Experimental results

- calibration curve
- pore size distribution

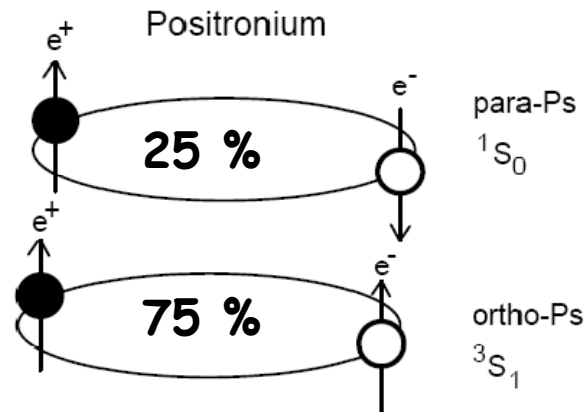
## ■ Summary



# Principles of PALS: pick-off annihilation

## positrons from $^{22}\text{Na}$ :

- thermalize, diffuse, being trapped and annihilate
- OR: positrons form Ps

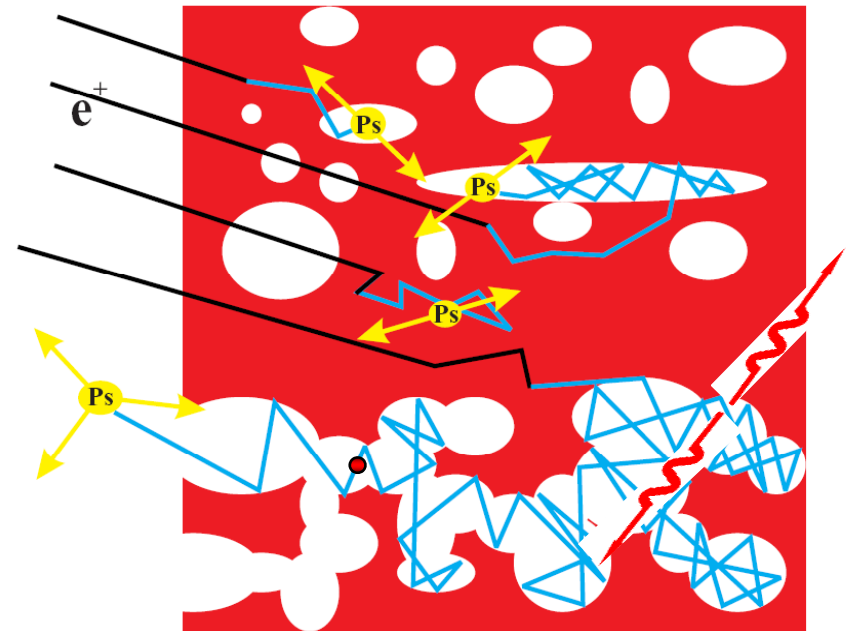


## positronium:

- p-Ps  $\rightarrow$  short self annihilation  
lifetime of 0.125 ns
- o-Ps  $\rightarrow$  long self annihilation  
lifetime of 142 ns ( $3\gamma$ )  
 $\rightarrow$  pick off annihilation ( $2\gamma$ )

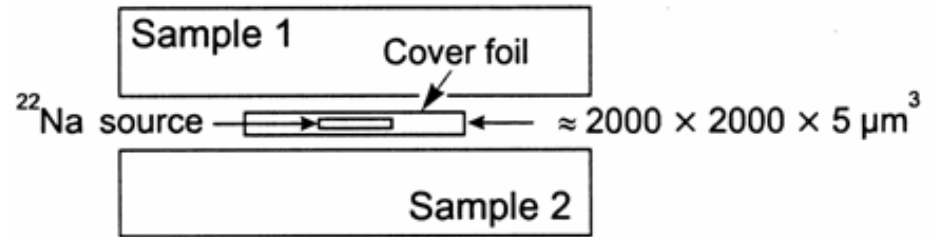
## pick-off annihilation:

- o-Ps captures  $e^-$  with anti-parallel spin
- happens during collisions at walls of pore
- lifetime ( $\tau$ ) decreases rapidly
- $\tau$  is function of pore size: 1.5 - 142 ns
- also for closed pore systems

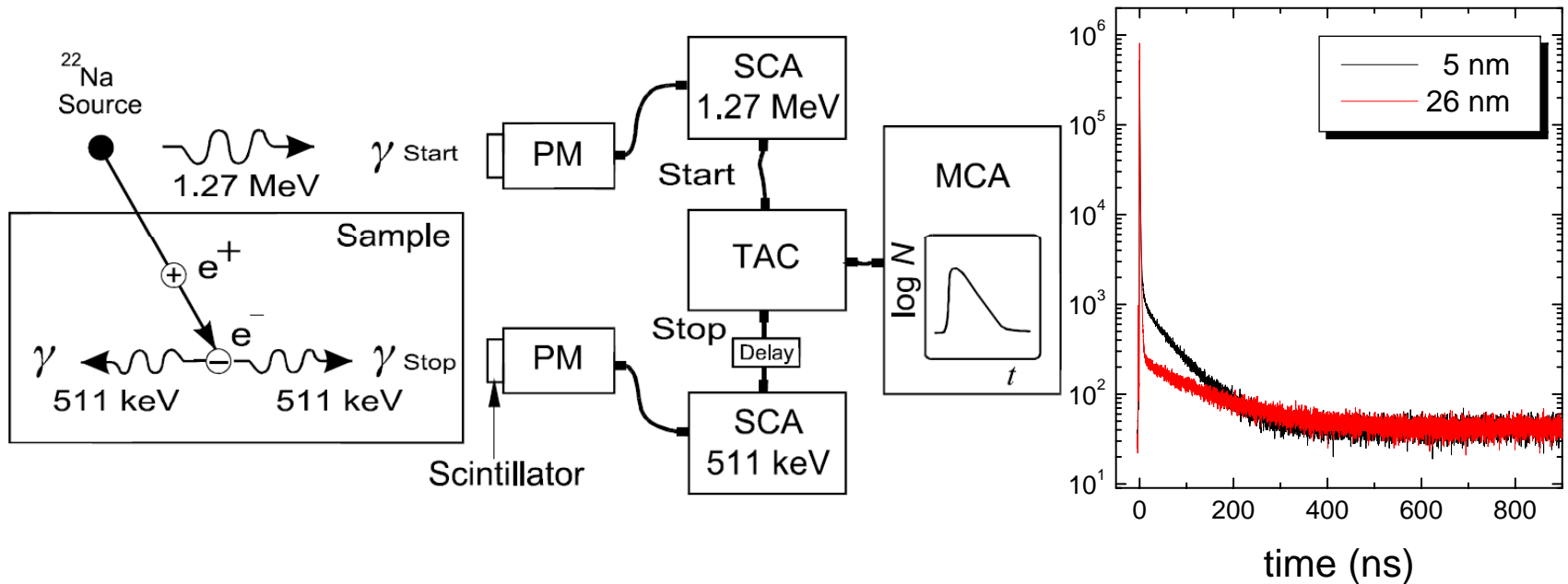


# Principles of PALS

- sample preparation: "sandwich"

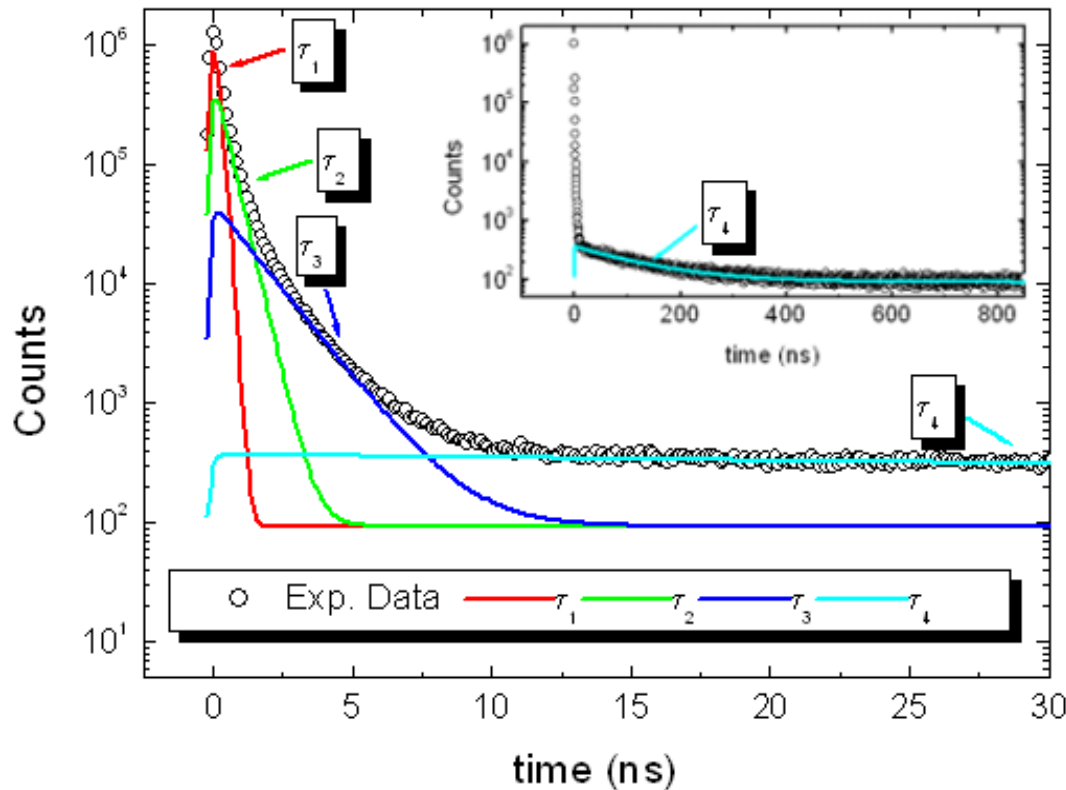


- positron(ium) lifetime: time between "birth" (1,27 MeV) and "death" (511 keV)



# Principles of PALS: typical spectrum

typical lifetime spectrum for CPG (here  $d = 20$  nm):



- 4 exponential decay components
- p-Ps  $\rightarrow$  0.125 ns
- free positrons  $\sim$  0.5 ns
- o-Ps in disordered structure  $\sim$  1.5 ns
- o-Ps in pores
- analysis with LT9 (LifeTime)

$$N(t) = \sum_{i=1}^{k+1} \frac{I_i}{\tau_i} \exp\left(-\frac{t}{\tau_i}\right)$$

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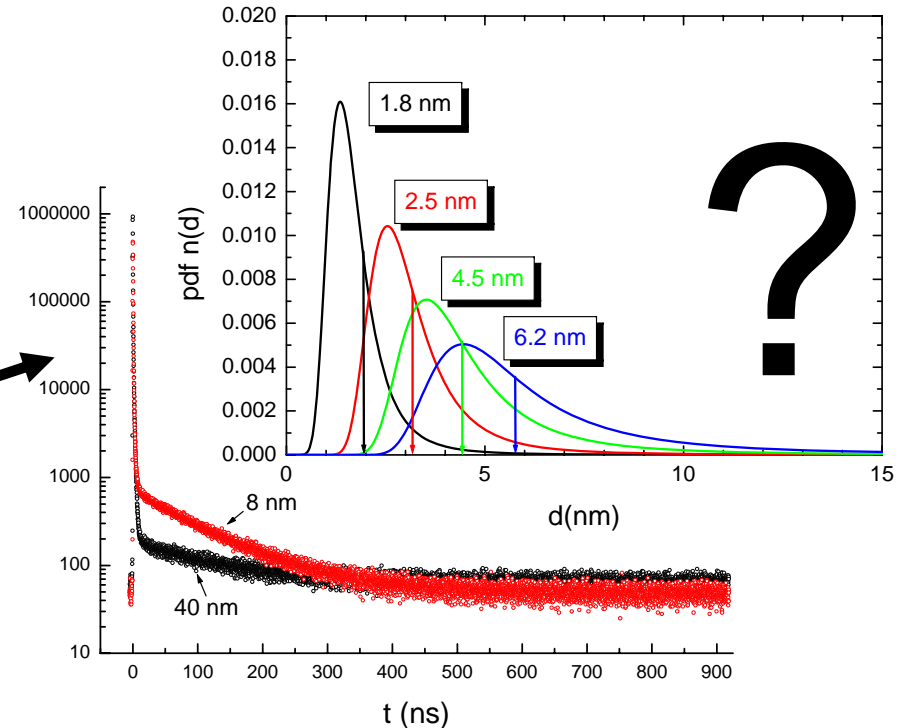
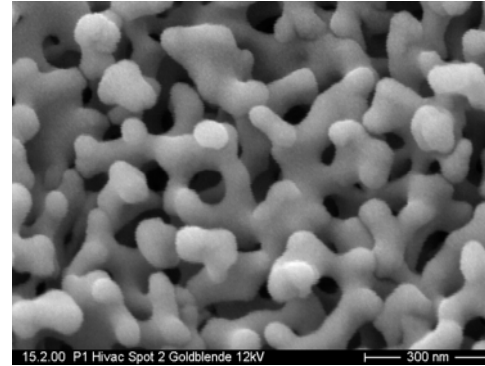
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# Why „nanopores“?

IUPAC (International Union of Pure and Applied Chemistry)

- micropores ( $D < 2 \text{ nm}$ )
- mesopores ( $D = 2 \dots 50 \text{ nm}$ )
- macropores ( $D > 50 \text{ nm}$ )

„nanopores“ in

- zeolithes
- glass (VYCOR, CPG)
- activated carbon filter

are useful for

- molecular filters
- low k film for microelectronics
- catalyst

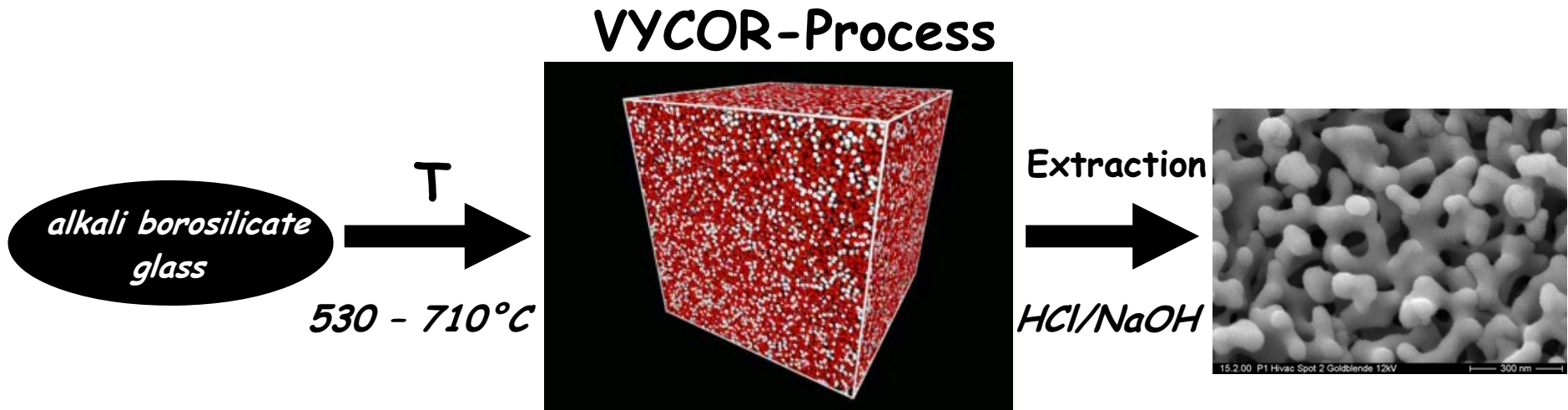
In literature most positron measurements on VYCOR.

We investigate controlled pore glass!

15.2.00 P1 Hivac Spot 2 Goldblende 12kV

300 nm

# Controlled pore glass - CPG

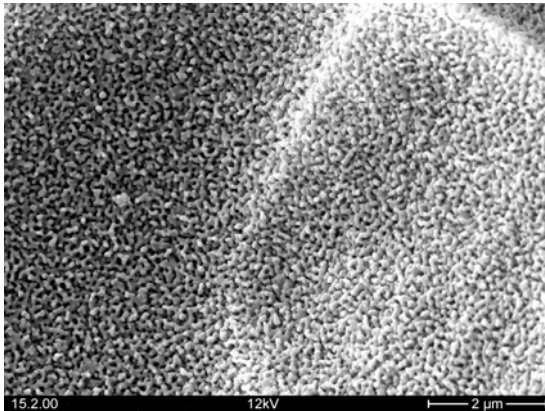


$d_p$  1 to 110 nm

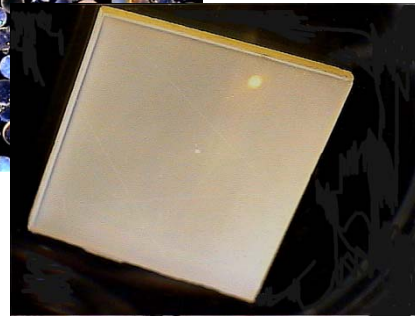
- spinodal phase separation
- decomposition is initiated by heat treatment
- alkali rich borate phase  $\leftrightarrow$  pure silica
- alkali phase soluble in acid  $\rightarrow$  silica network
- pore size depends on basic material
- porosity of 50 %



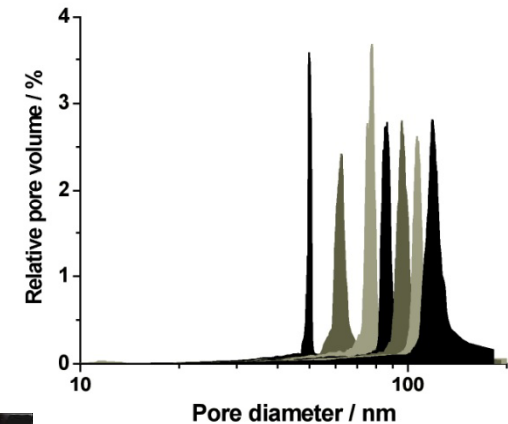
# Controlled pore glass - CPG



- different geometries possible



- homogenous microstructure
- uniform pore size



- controlled pore size
- we can choose  $d$  (!)

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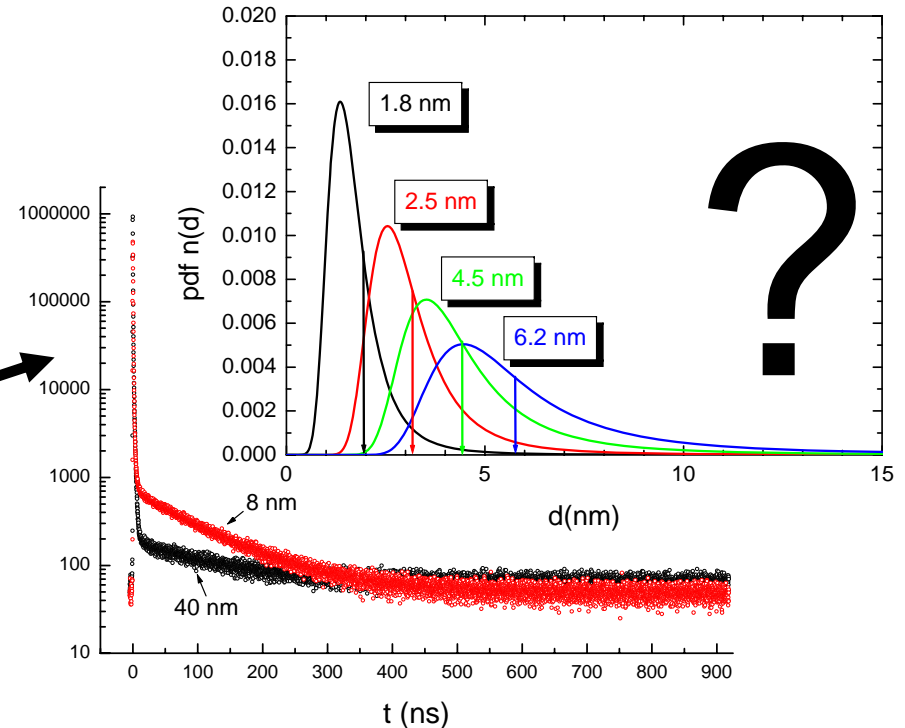
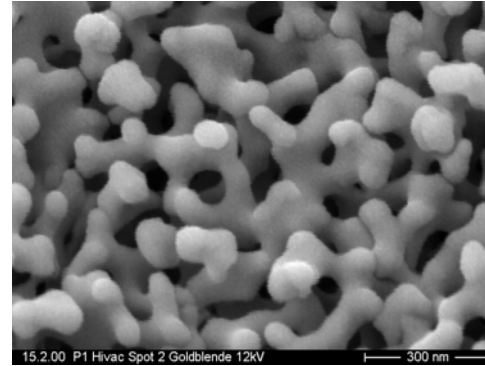
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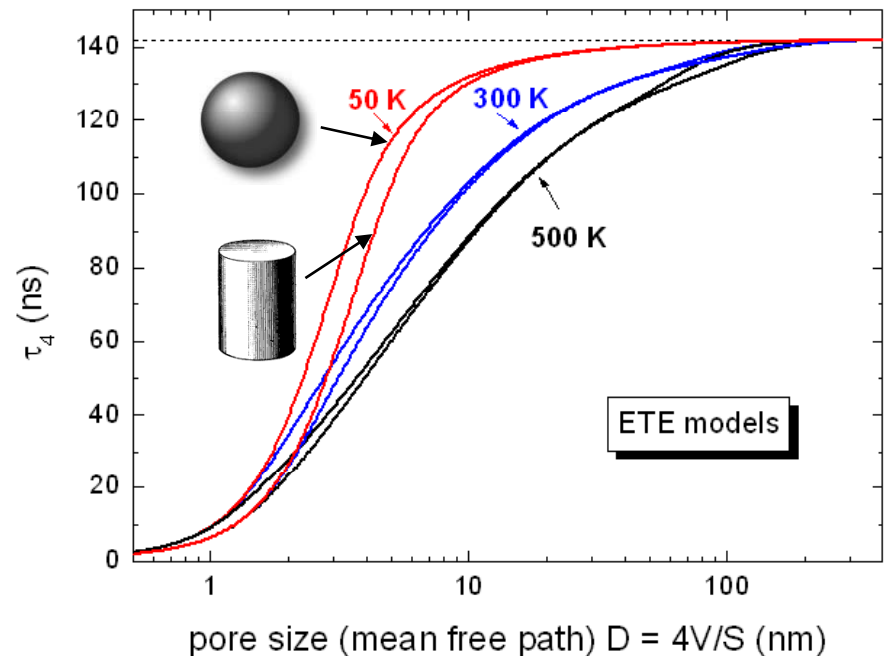
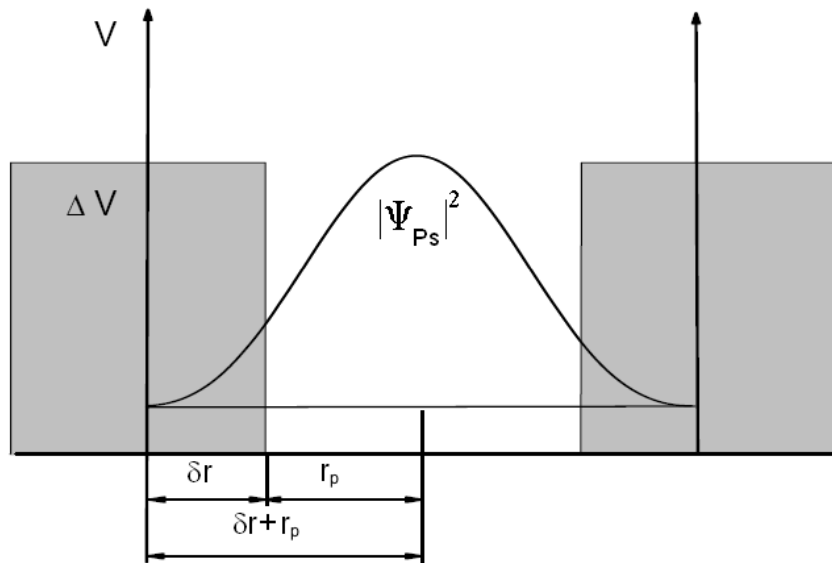
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# Extended Tao Eldrup model

- extended TE model (calculations by EELViS):
  - quantum well of infinite height, but: overlap of o-Ps wave function and wall of pore  $\rightarrow \delta$
  - Boltzmann statistics ascribes explicit temperature dependence to the lifetime
  - integrals of spherical / cylindrical Bessel functions
  - $\delta = 0.19$  nm
  - mean free path  $D = 4V/S = d_{\text{cyl}}$ , diameter of cylinder
  - mean free path  $D = 4V/S = 2/3 d_{\text{sphere}}$ , diameter of sphere



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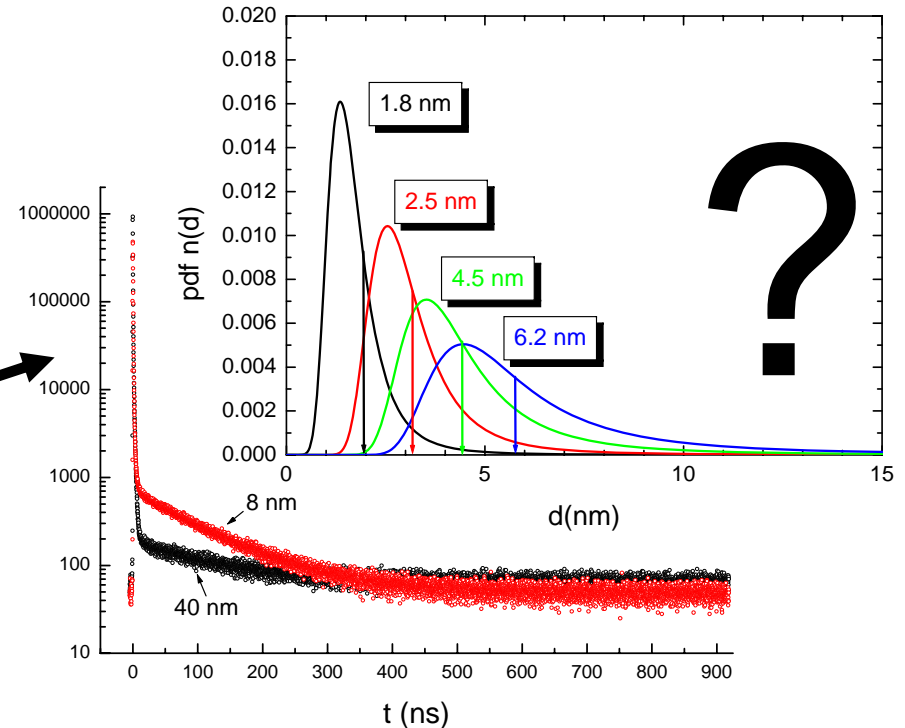
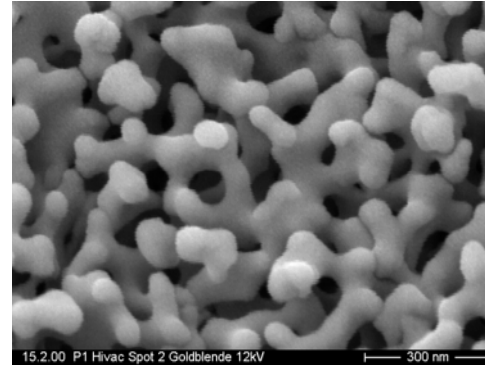
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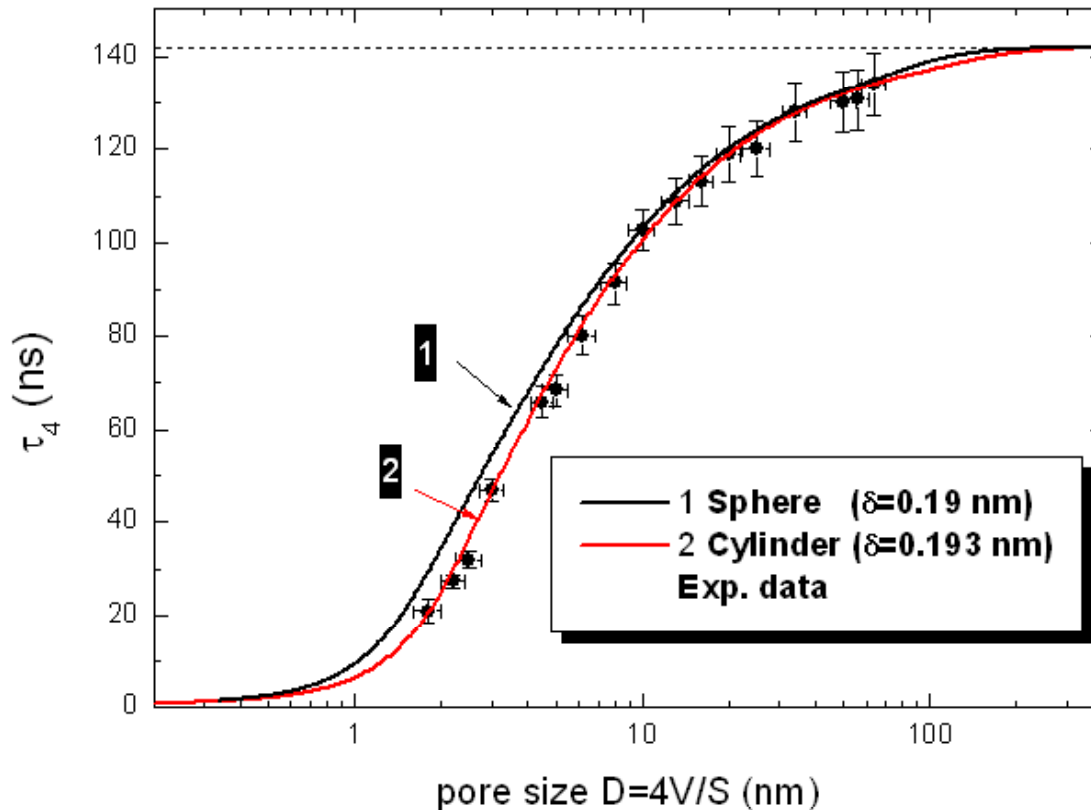
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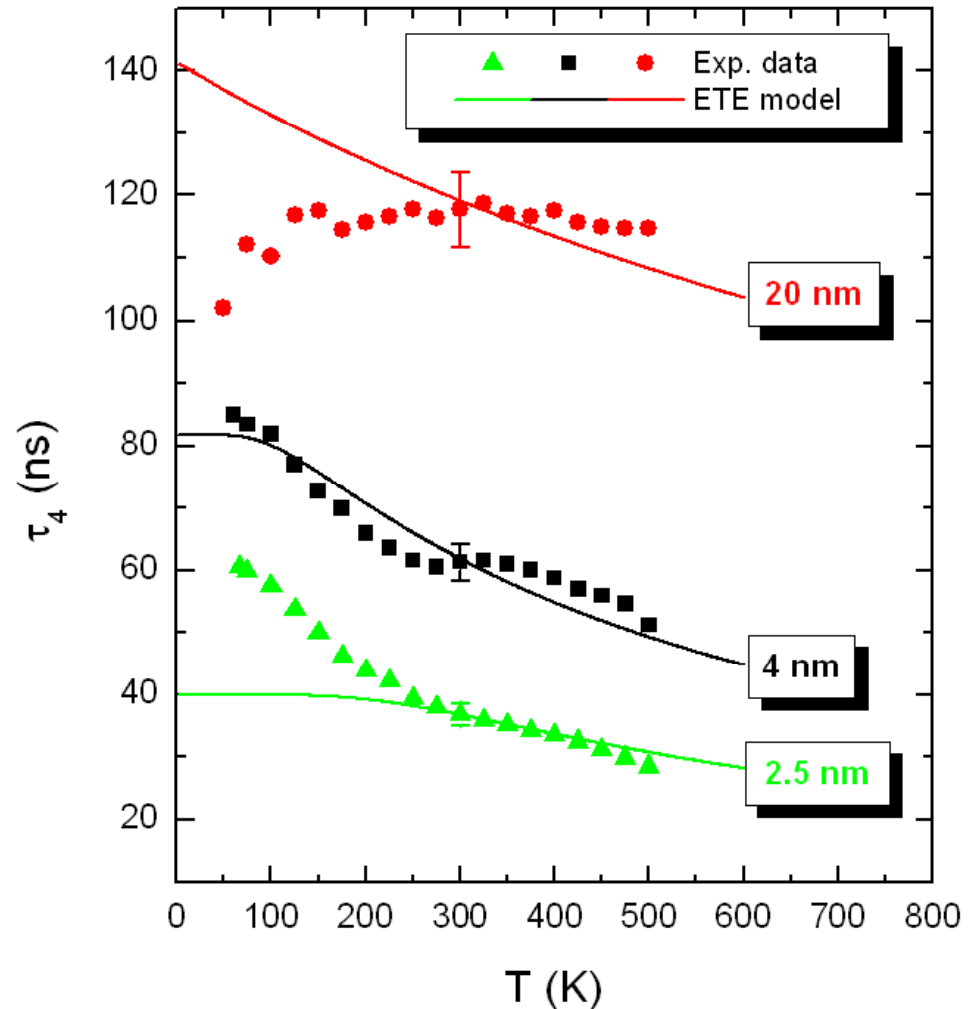
# The experiments at $T = 300\text{ K}$



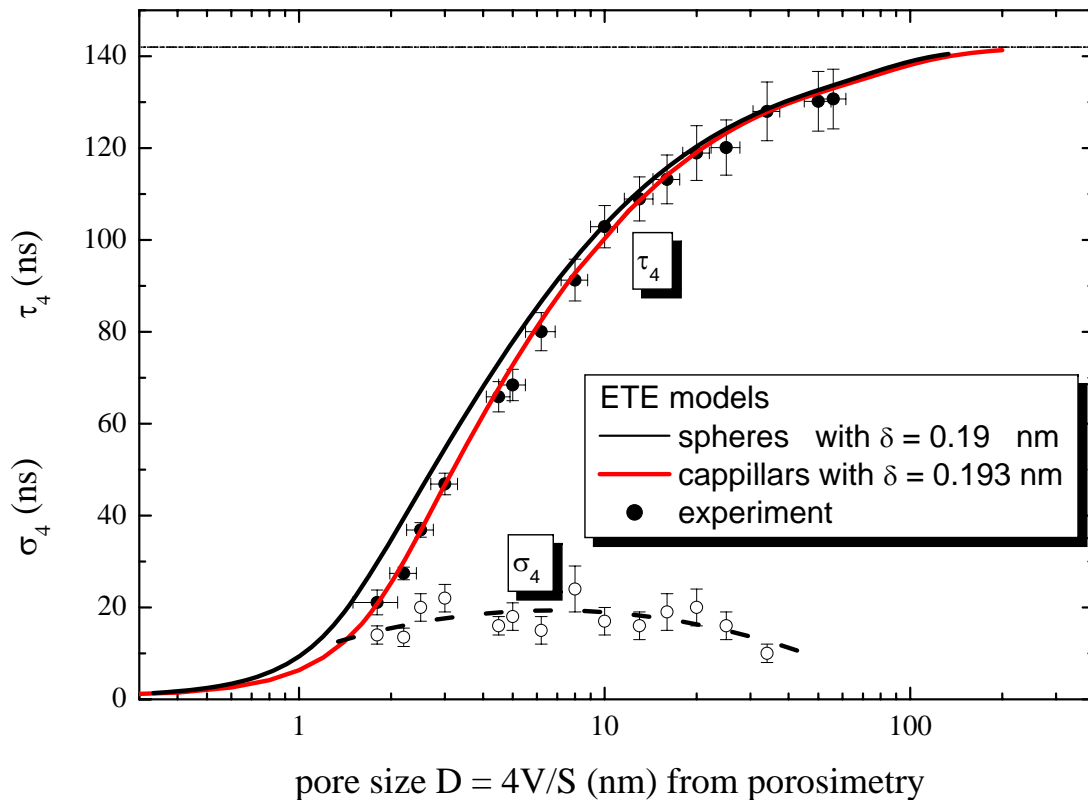
- we measured CPG in a broad pore size range
- given pore sizes obtained by  $\text{N}_2$ -adsorption or Hg-intrusion
- $\delta = 0.193\text{ nm}$  best fit for our CPG -> calibration curve for calculating pore size
- good model for  $T = 300\text{ K}$ , also good model for temperature dependence of lifetime?

# The T-dependence

- **calculations:** cylindric model with  $\delta = 0.193$  nm
- although we found good agreement for  $T > 300$  K temperature behavior cannot be explained very well at low temperatures
- for 20 nm a catching effect of o-Ps at low temperatures may occur (van-der-waals power, "capillary condensation") and o-Ps bonds at the wall
- model still too simple but works well for room temperature



# Pore size distribution



D	$\tau_4$	$\sigma_4$
1.8 nm	21.1 ns	14.8 ns
2.5 nm	46.9 ns	17.6 ns
4.5 nm	65.9 ns	18.9 ns
6.2 nm	80.0 ns	19.3 ns

- $\tau_4$  and its distribution  $\sigma_4$  by analysis of truncated spectra starting from 20 ns
- **problem of LT: limit of 142 ns is not taken into account, for large pores unphysically large  $\sigma_4$**
- distribution for 4 smaller selected pores

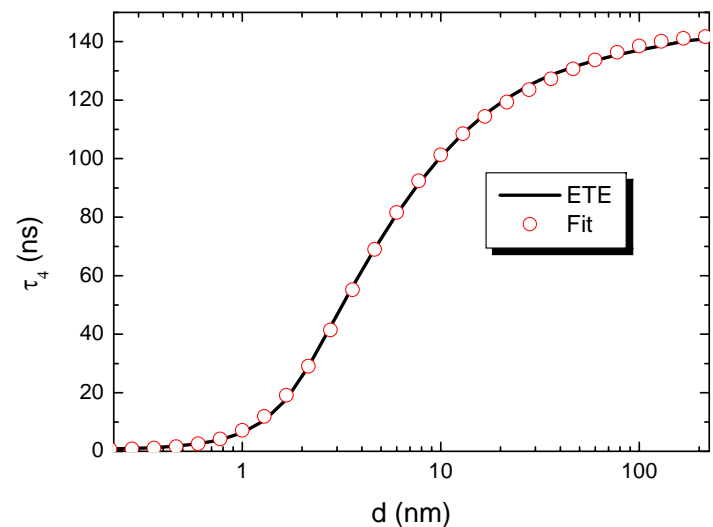
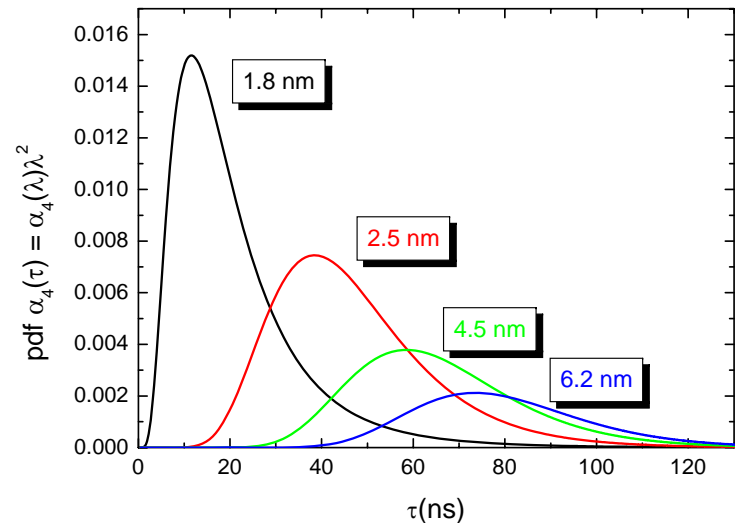
# Pore size distribution

- **distribution of  $\tau_4$ :  $\alpha_4(\tau) = \alpha_4(\lambda)\lambda^2$ ,**  
 $\alpha_4(\lambda)$  is probability density function (pdf) of o-Ps annihilation rate, assumed by LT to be a log. Gaussian
- **from distr.  $\alpha_4(\tau)$  it is possible to calc. distribution of diameters of the pore:**

$$n(d_{cyl}) = \alpha_4(\tau) \left( \frac{d\tau_4}{dd_{cyl}} \right)$$

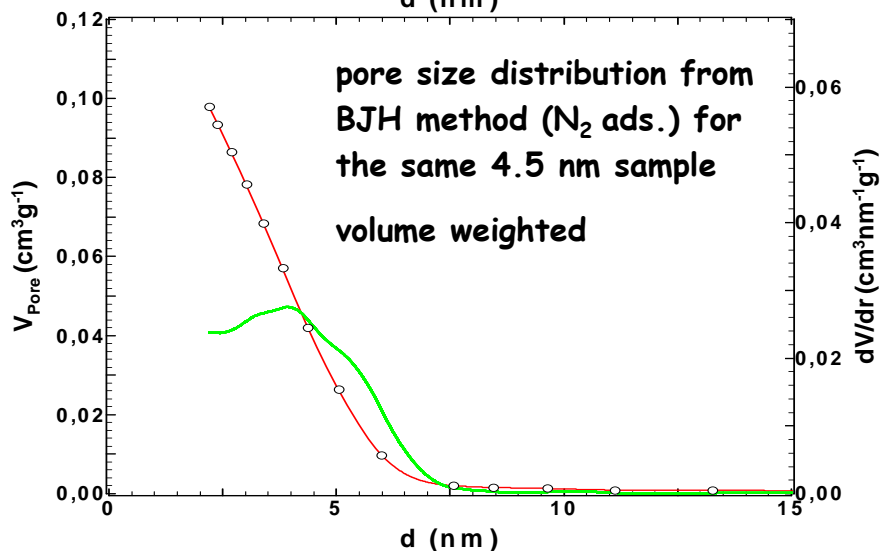
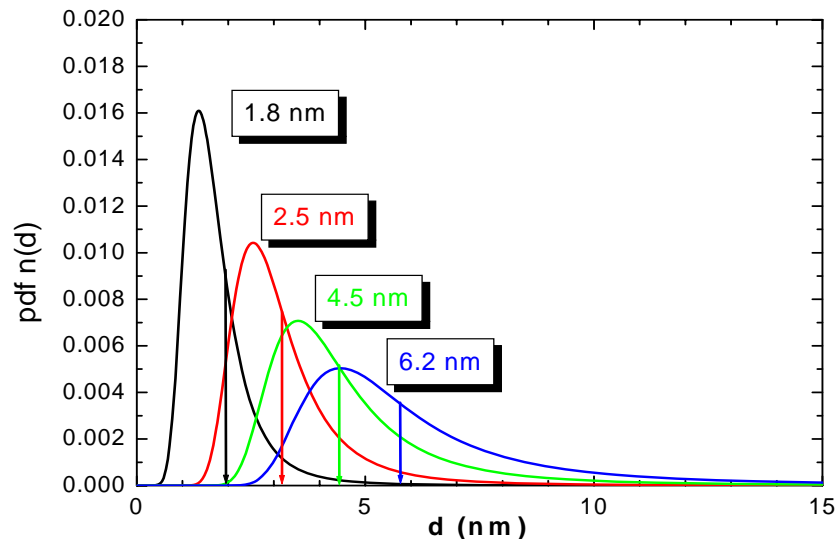
- **all we need is a differentiable analytical function  $\tau_4 = \tau_4(d_{cyl})$ :**

$$\tau_4 = A_2 + \left( \frac{A_1 - A_2}{1 + (d_{cyl} / d_{cyl0})^p} \right)$$





# Pore size distribution



- distribution norm. to 1
- arrows show  $d$  directly calculated from mean o-Ps lifetime using cylindric model (1.77 nm, 3.09 nm, 4.38 nm and 5.80 nm)
- this distribution contains the true variation of pore sizes but also the effect of irregular not linear character of pores
- long tail for larger pores:
  - overestimation of  $\alpha_4(\tau)$
  - nonlinear char.  $\tau_4$  vs.  $d$

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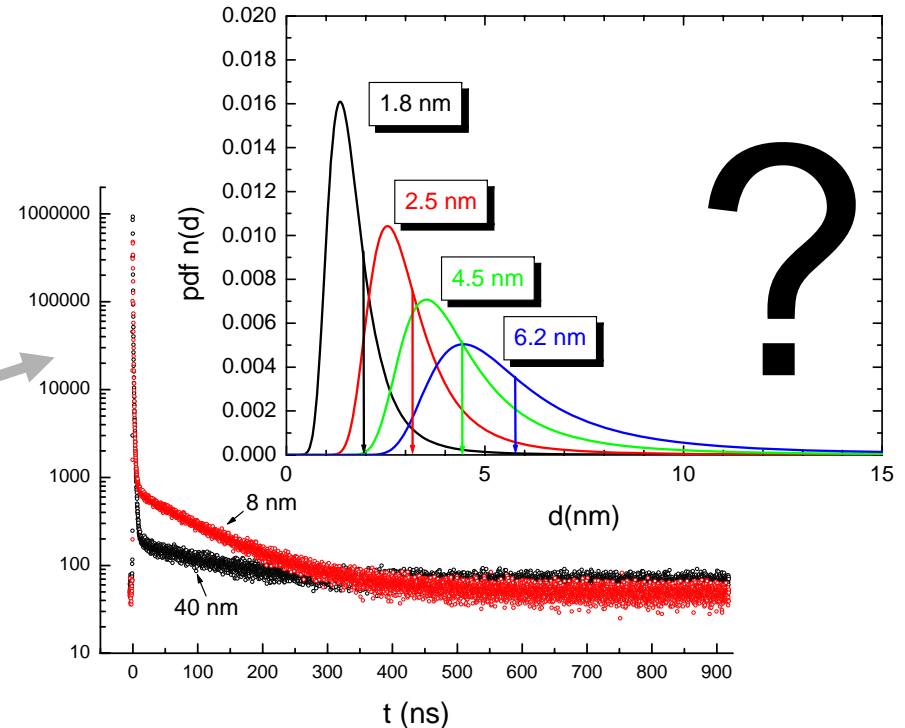
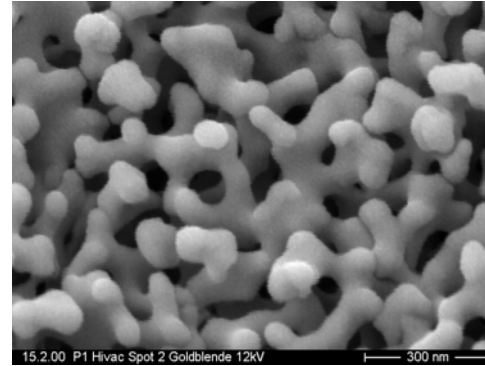
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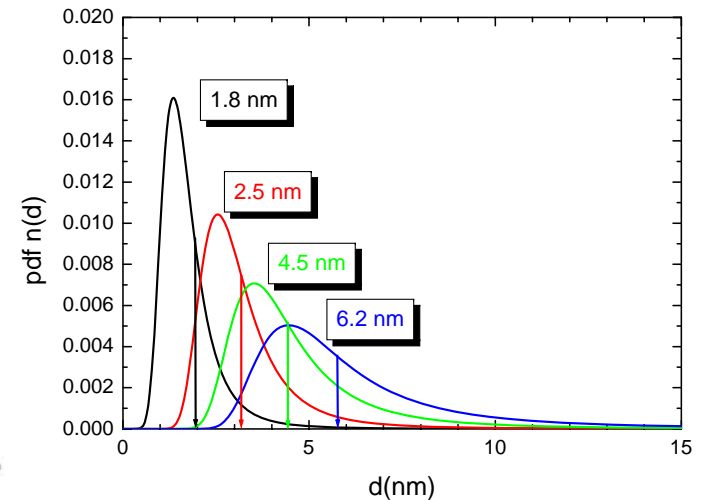
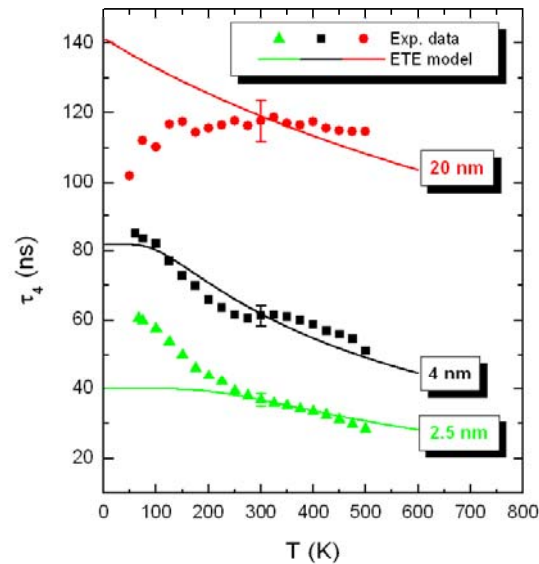
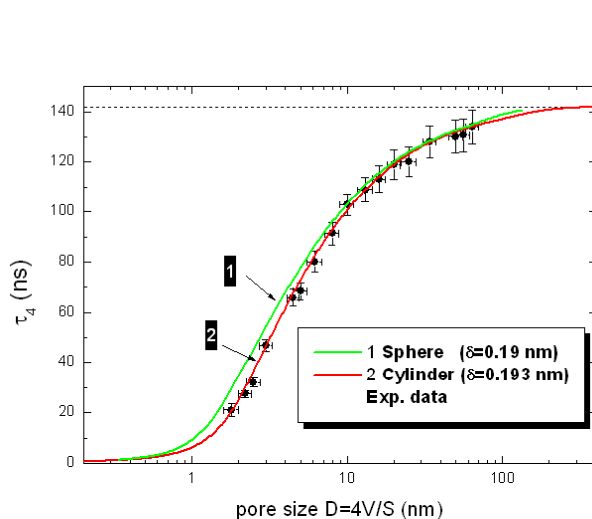
- √  calibration curve
- √  pore size distribution

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# Summary

- for  $T = 300$  K we found a calibration curve for CPG
  - non destructive porosimetry tool for opened and closed pore-systems
  - most sensitive for  $d = 0.5 \dots 10$  nm
- for other temperatures the measurements show disagreement to the ETE model -> model still too simple
- for pores  $d < 10$  nm we can calculate a pore size distribution
- near future:
  - phase transition of gas in CPG (to be presented @ PPC9 Wuhan / China, May 2008)
  - SBA-15 (to be presented @ COPS VIII Edinburgh / Scotland, June 2008)



# Acknowledgment

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- R. Zaleski and his group (Lublin/Poland) for EELViS
- G. Dlubek (Halle/Germany) for fruitful discussions
- FZD

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- Thanks for your patience!

- This talk as pdf?

- <http://positron.physik.uni-halle.de>