

# Free Volume of Polymers using Positron Annihilation Lifetime Spectroscopy (PALS)

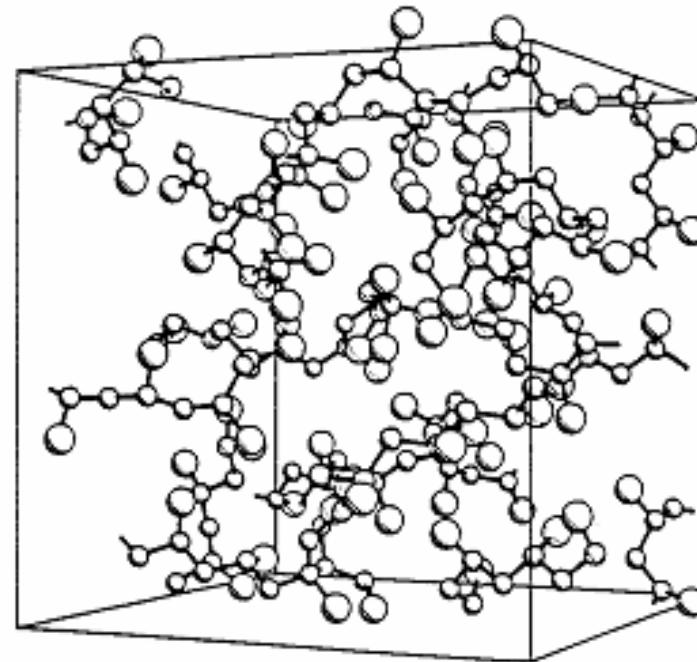
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# Structure of the free volume

- free volume due to structural, static or dynamic, disorder
- important for several macroscopic properties of these materials,
- viscosity, molecular transport, structural relaxation, and physical aging



Schematic representaion of a  
single Poly (Propylene)  
microstructure (X=76)

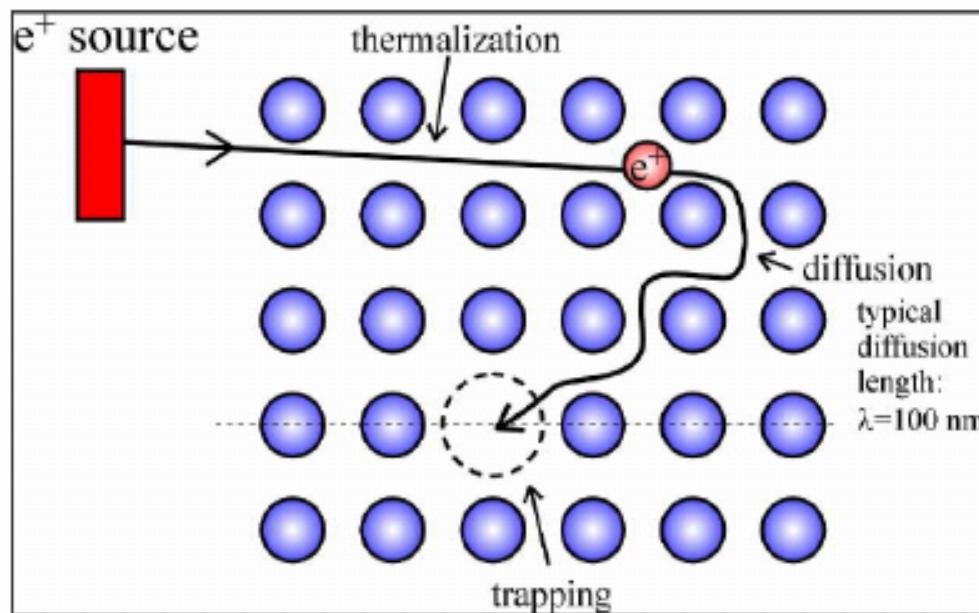
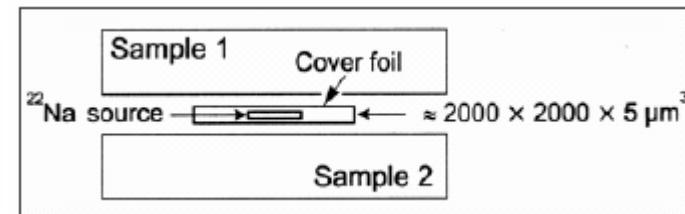
(Simulation, Theodorou et al. 1985)

# Experimental Ways to determine Free Volume in Polymers

- **Positron Annihilation Lifetime Spectroscopy (PALS)**
    - Detection of subnanometric local free volumes (holes): Size distribution (mean hole volume  $\langle v_h \rangle$  and mean dispersion  $\sigma_h$ )
  - **Pressure-Volume-Temperature-Experiments (PVT)**  
Analysis by Simha-Somcynsky lattice-hole model EOS
    - Fraction of vacancies  $h$ , specific hole free.  $V_f = hV$ , and occupied volumes,  $V_{occ} = (1-h)V$
  - **Correlation of PALS and PVT**
    - allows estimation of PALS hole density  $V_f = N_h \cdot \langle v_h \rangle$
- All parameters of the structure of hole free volume can be obtained from PALS and PVT

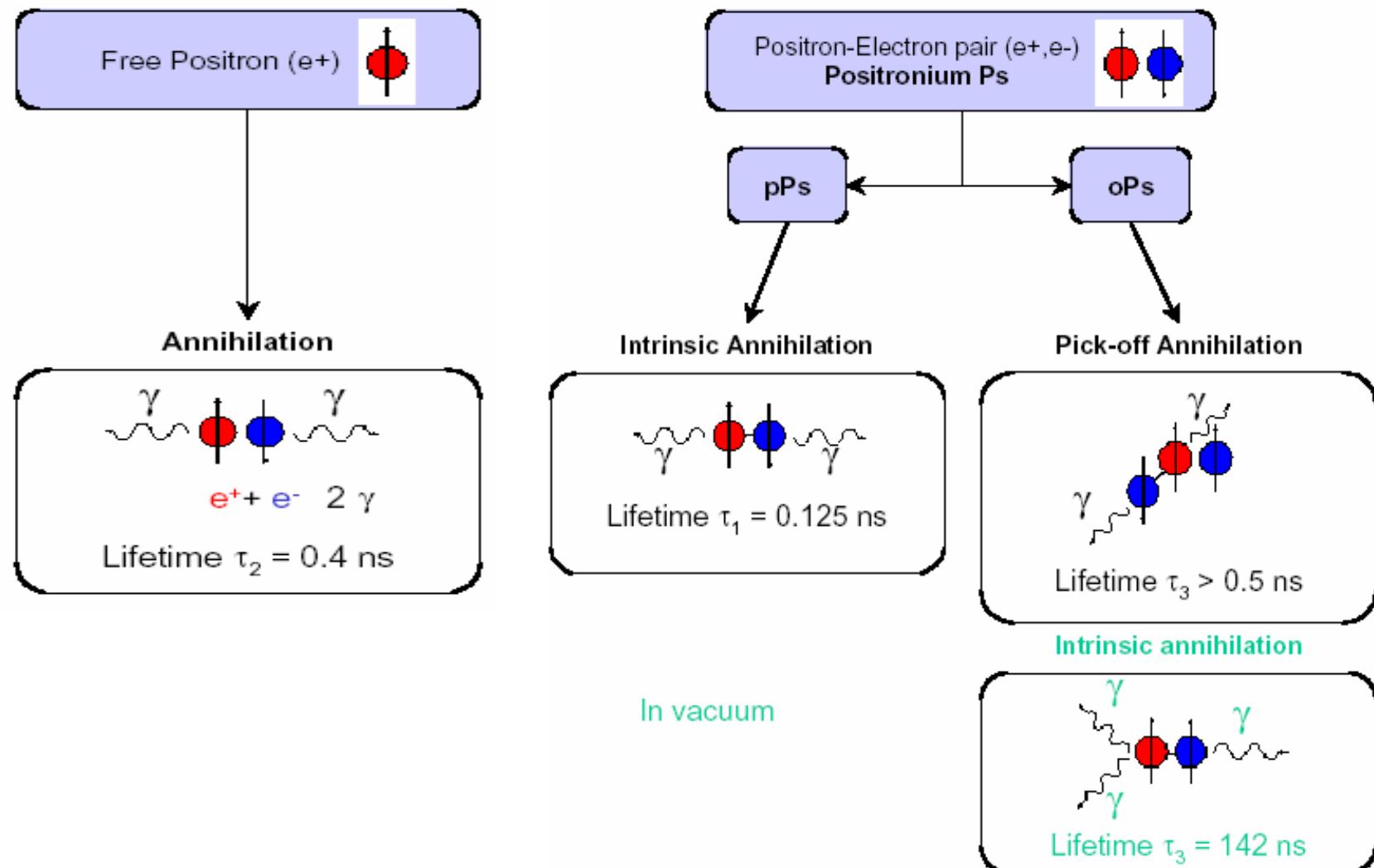
# Basics of PALS

- $\beta^+$  decay:  $^{22}\text{Na} \rightarrow ^{22}\text{Ne} + \beta^+ + \nu_e + \gamma_{(1.27\text{MeV})}$   
(half life: 2.6 years, up to  $10^6 \text{ e}^+/\text{s}$ )

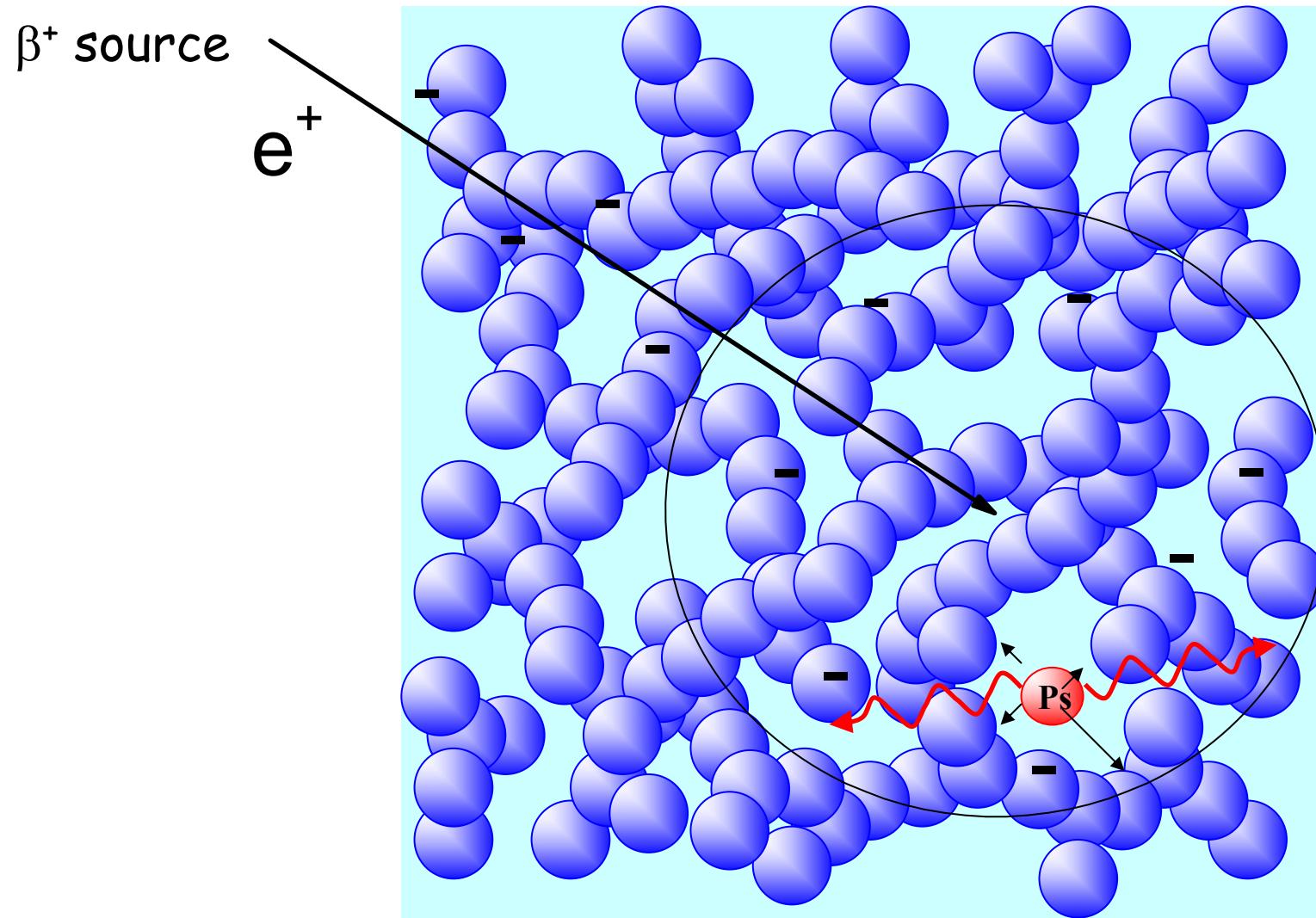


- Thermalization
- Diffusion
- Annihilation

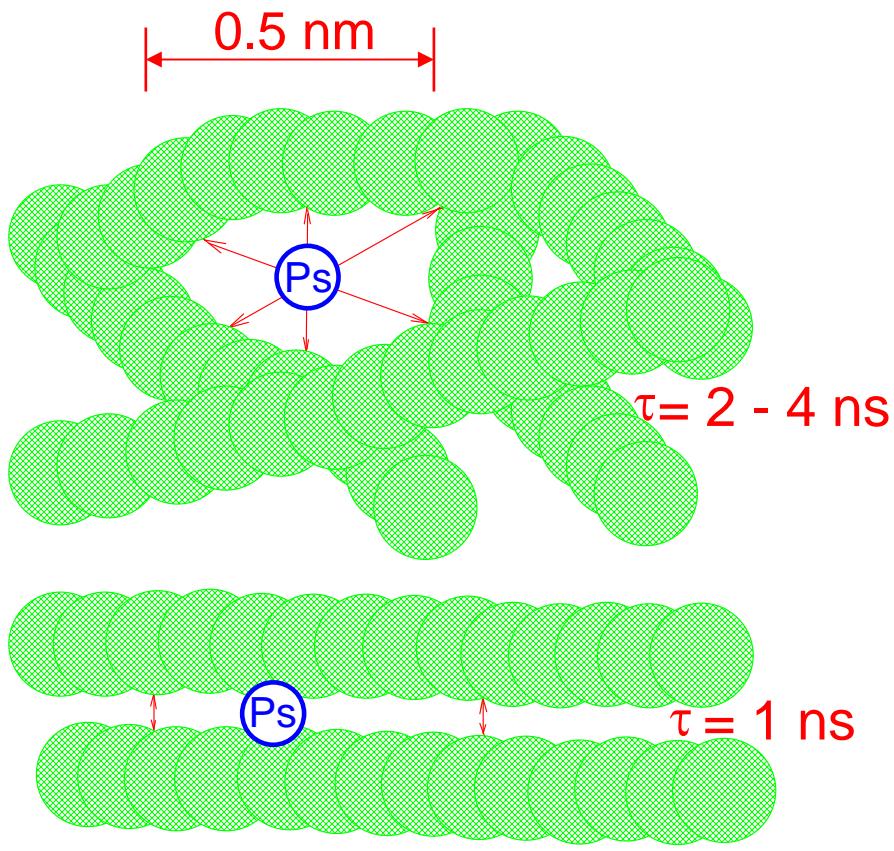
# Basic Principles and Theories of Positron formation in Polymers



# Ps Formation in Polymers



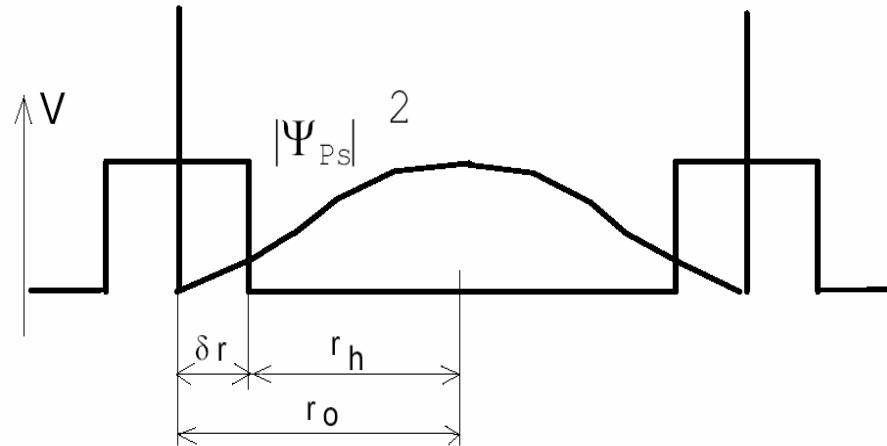
# Pick-Off Annihilation



Ps localization in a hole  
of the (excess) free  
volume

Ps localization in  
interstitial free volume  
gives the packing co-  
efficient 'C' of the  
crystals

# Theory of Tau-Eldrup (TE) Model



The height of the potential is infinity, and  $\delta r$  - empirical parameter  $\delta r = 0.166 \text{ nm}$

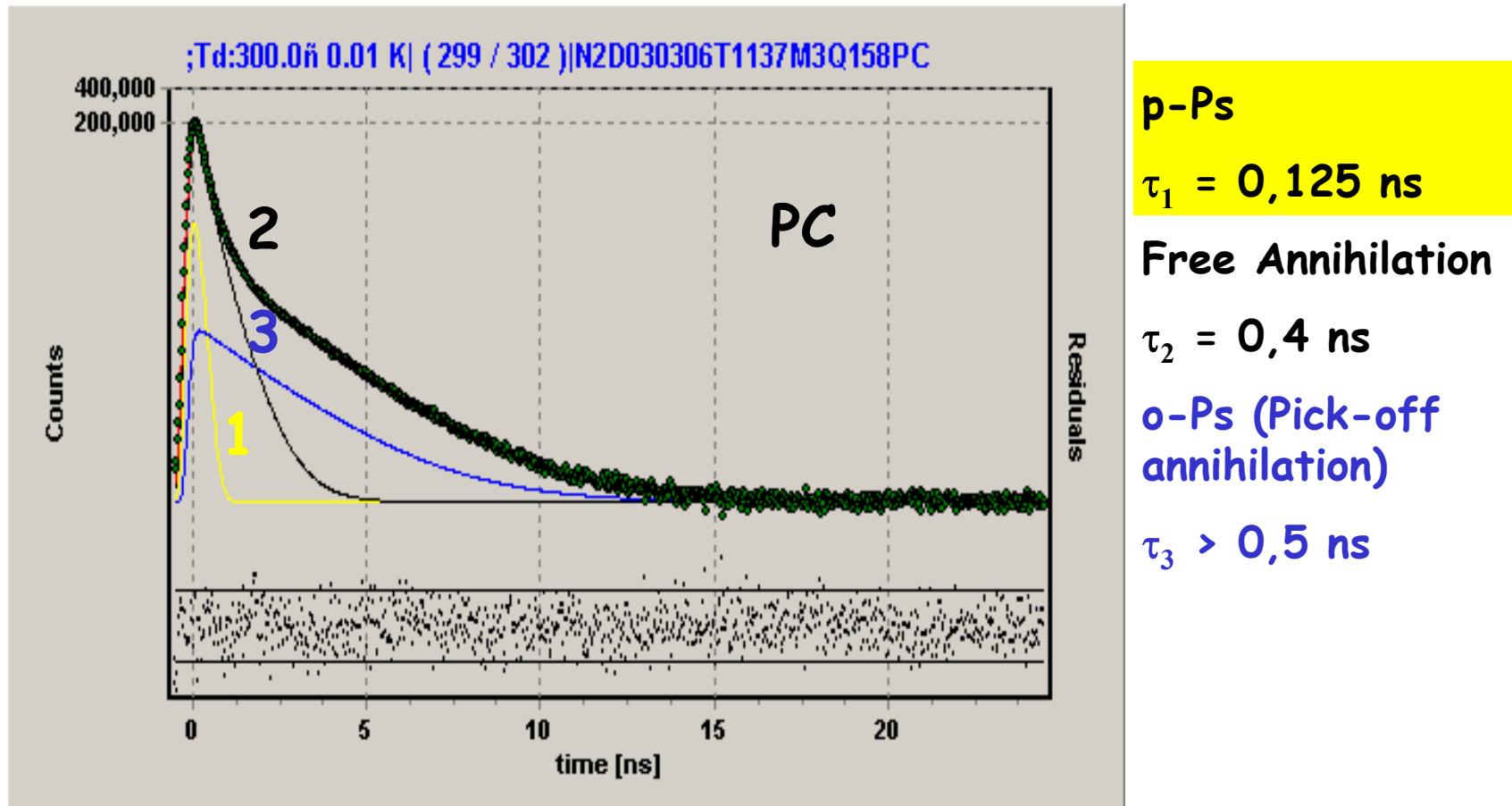
$$\tau_{o-Ps \text{ pickoff}} = \frac{0.5 \text{ ns}}{\left[ 1 - \frac{r_h}{r_h + \delta r} + \frac{1}{2\pi} \sin\left(\frac{2\pi r_h}{r_h + \delta r}\right) \right]}$$



**mean hole volume**

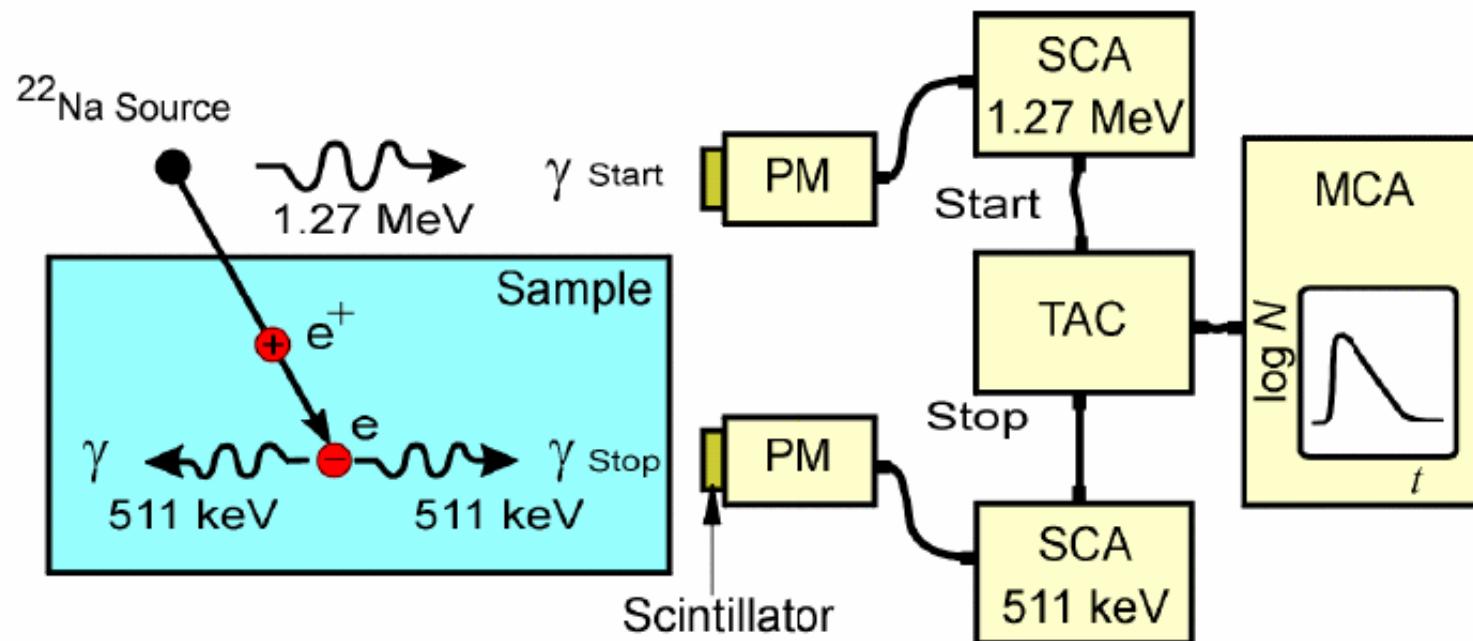
$$v_h(\tau_3) = (4/3)\pi r_h^3(\tau_3)$$

# Typical PALS Spectrum



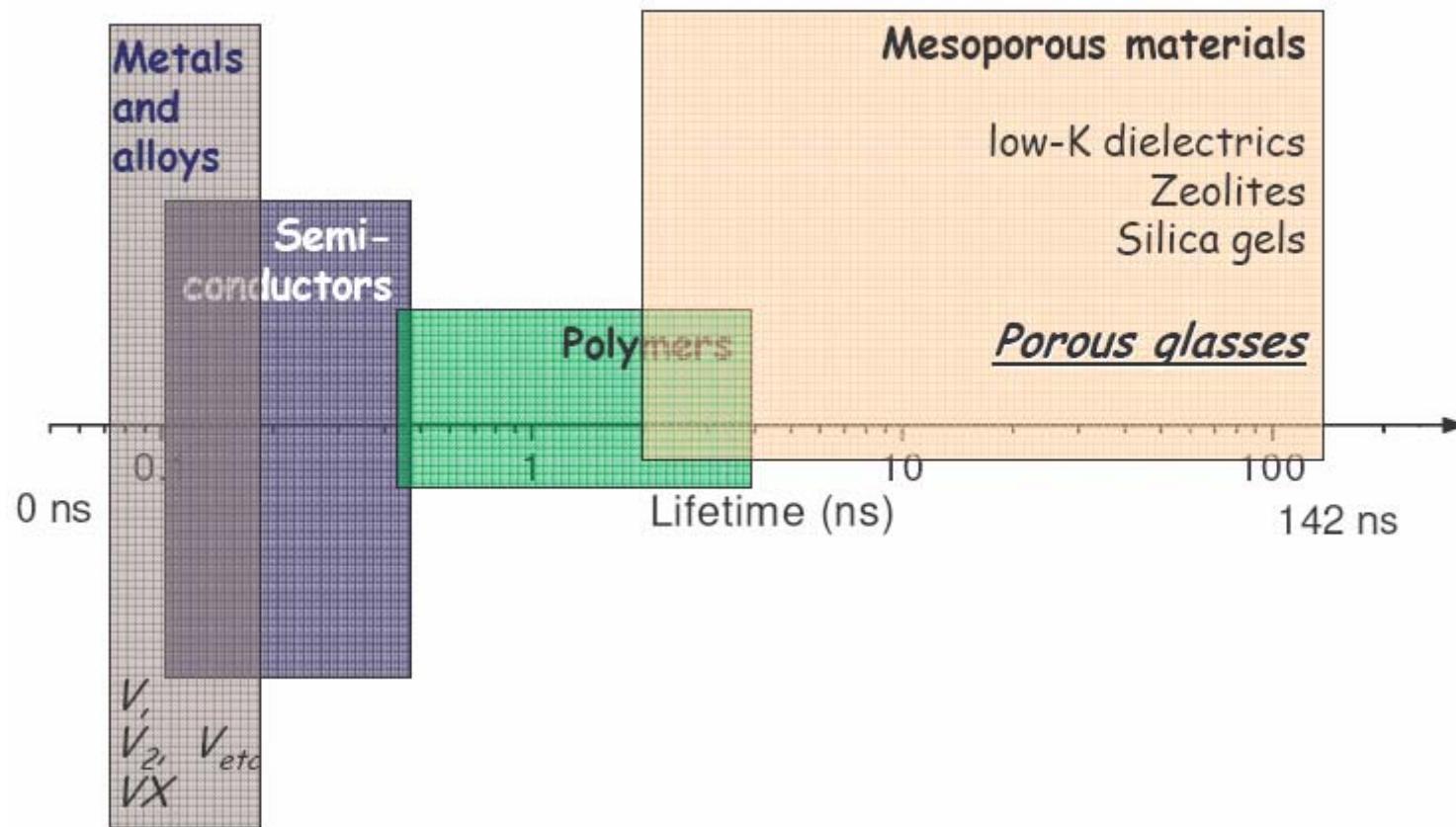
$$n(t) = I_1 \exp(-t/\tau_1) + I_2 \exp(-t/\tau_2) + I_3 \exp(-t/\tau_3)$$

# The Positron Lifetime Measurement

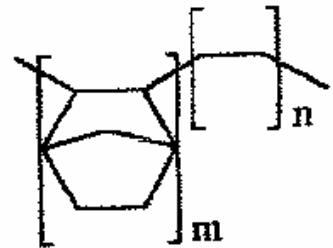


- Positron lifetime is measured as time difference between 1.27 MeV quantum ( $\beta^+$  decay) and 0.511 MeV quanta (annihilation process)
- PM=photomultiplier; SCA=single channel analyzer (constant-fraction type); TAC=time to amplitude converter; MCA= multi channel analyzer

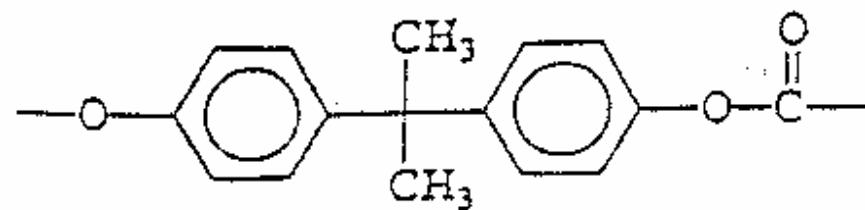
# Typical Lifetimes in Holes of:



# Analysis of COC and PC by PALS

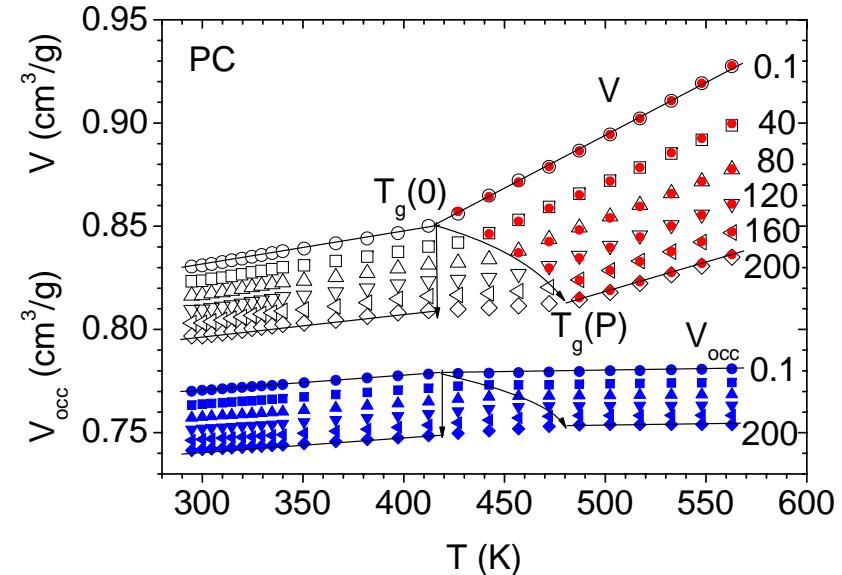
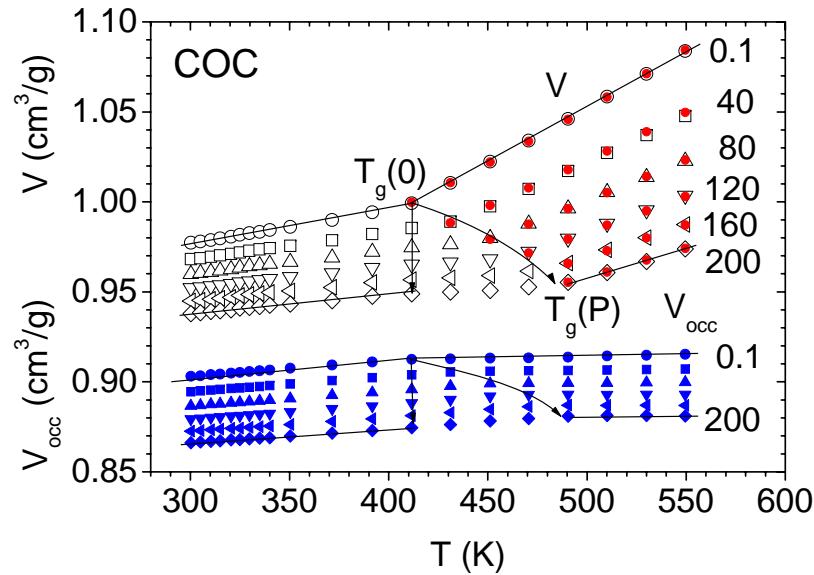


Cyclic Olefin Copolymer (COC)



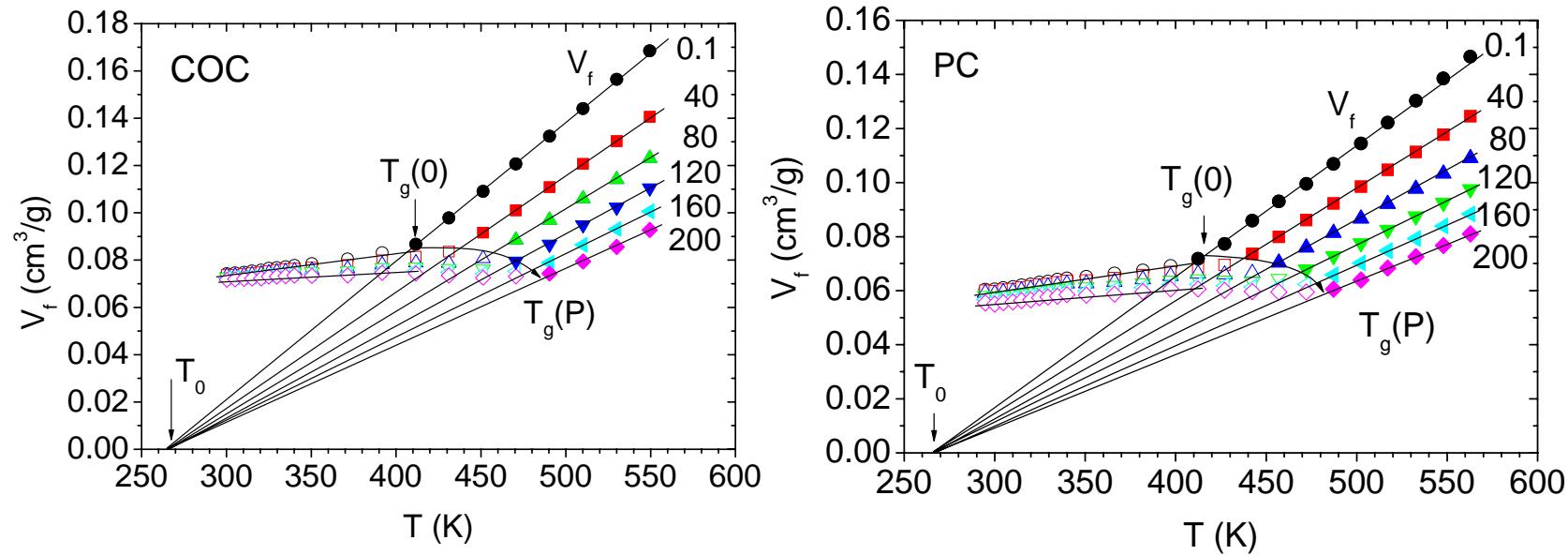
Poly Carbonate (PC)

# $V$ and $V_{occ}$ vs $T$ (K) [PVT]



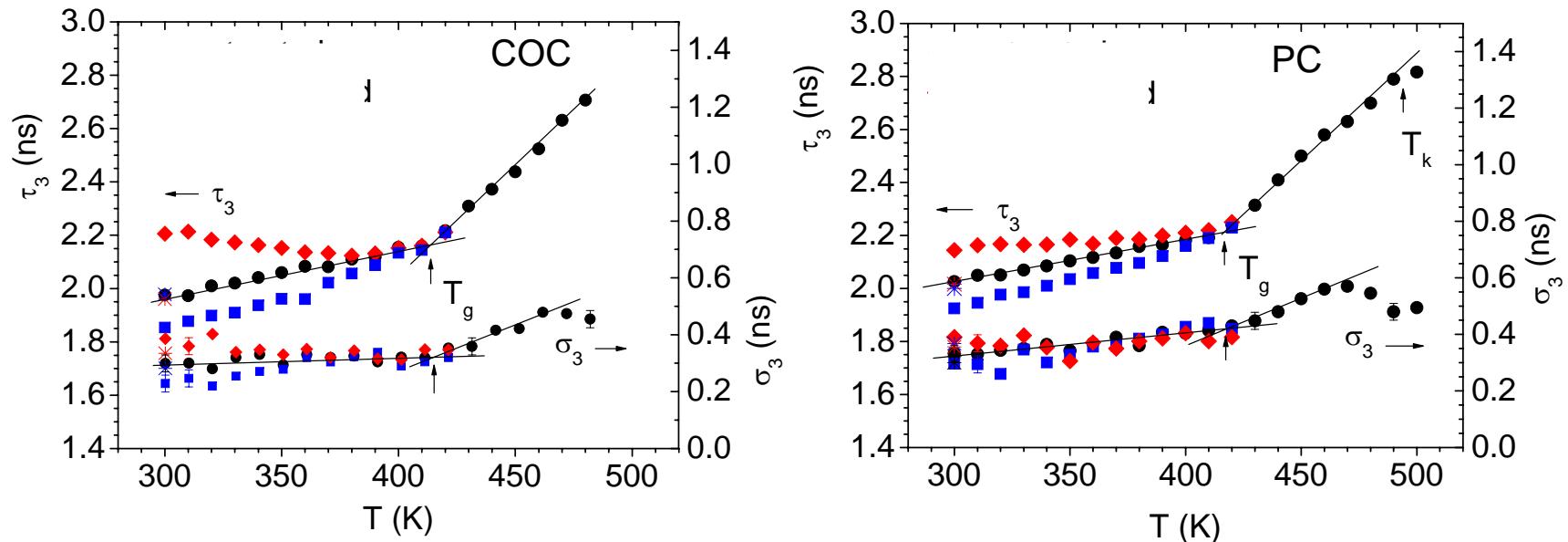
The specific total,  $V$ , (black open symbols), and occupied,  $V_{occ} = (1 - h)V$  (blue symbols) volume as a function of temperature  $T$  and as selection of isobars ( $P$  in MPa) for COC and PC.

# $V_f$ vs $T(K)$



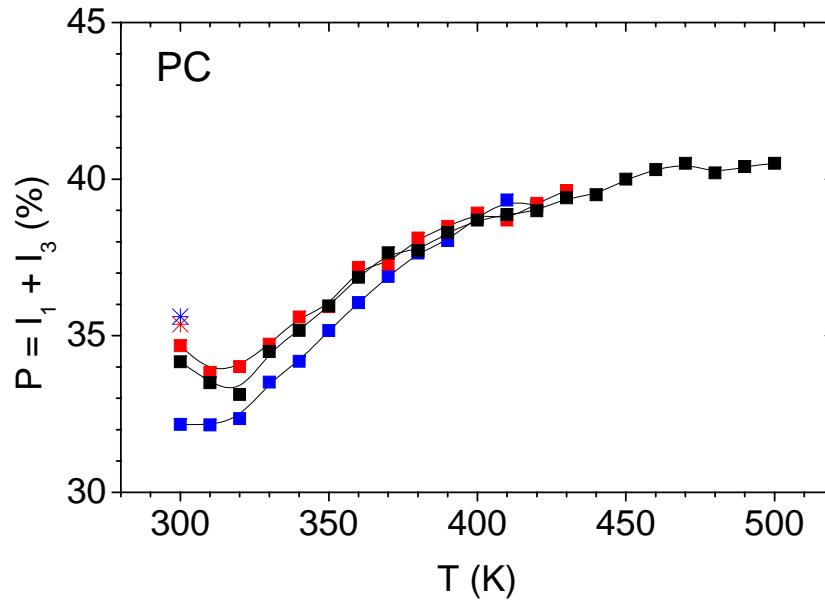
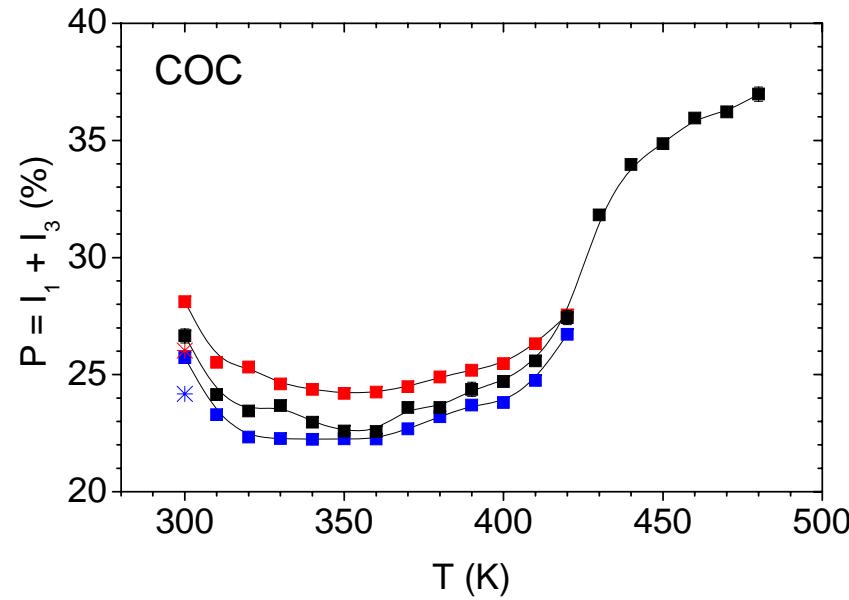
The specific hole free volume  $V_f = hV$  as a function of temperature  $T$  and as selection of isobars ( $P$  in MPa) for COC and PC.

## $\tau_3$ and $\sigma_3$ vs T (K) [PALS]



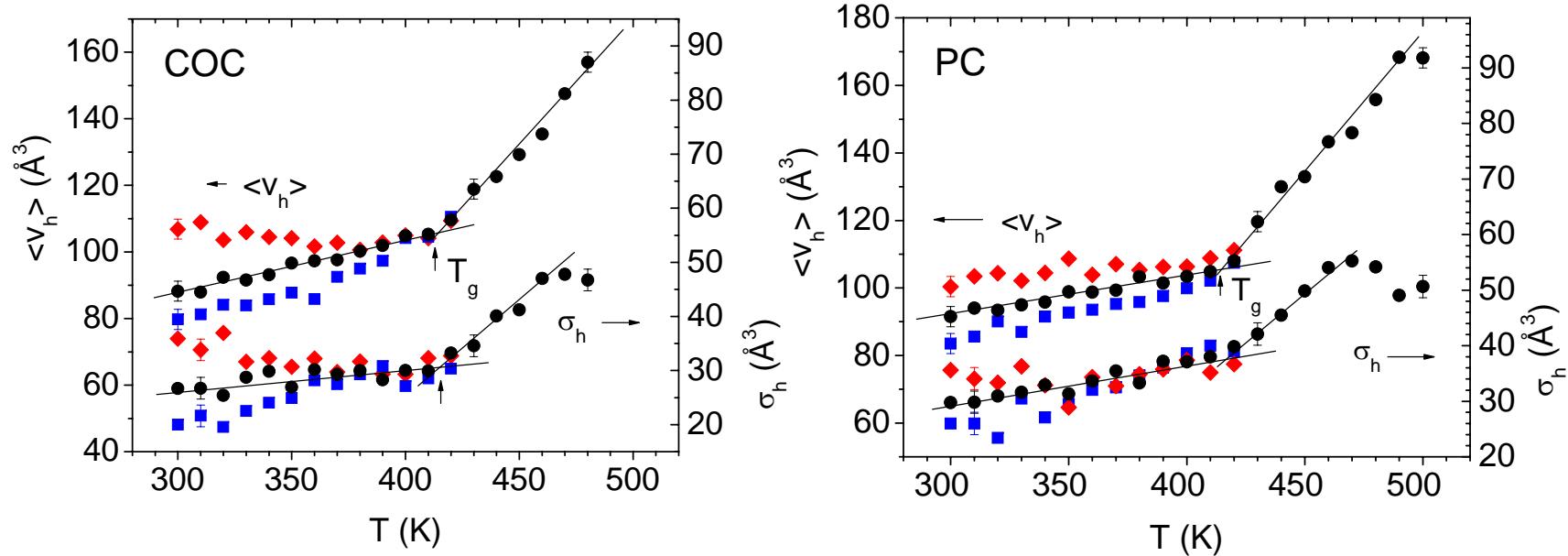
The mean,  $\tau_3$ , and the mean dispersion,  $\sigma_3$ , of o-Ps lifetimes as a function of temperature  $T$  for densified at 200 Map (blue), gas-exposed (read) and untreated (black) COC and PC.

# Ps yield vs T(K)



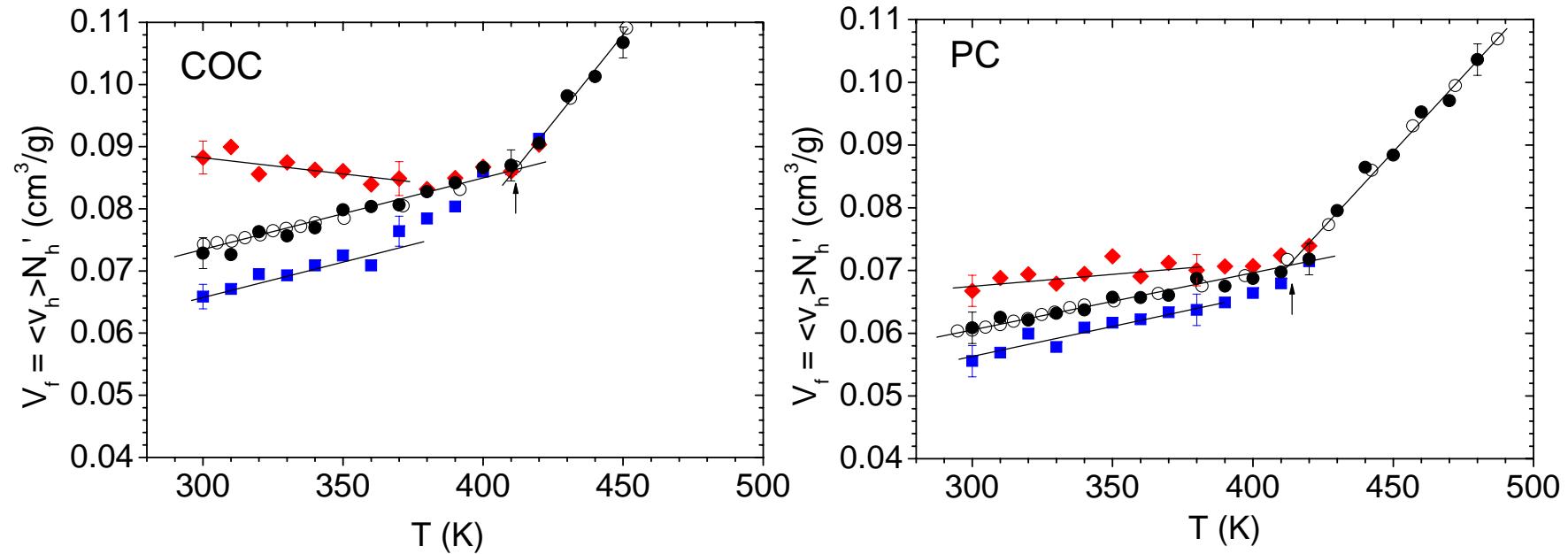
The Ps yield  $P = I_1 + I_3$  with  $I_1/I_3 = 1/3$  as a function of temperature  $T$  for densified at 200 Map (blue), gas-exposed (read) and untreated (black) COC and PC.

# $V_h$ and $\sigma_h$ vs T(K)



The mean,  $\langle v_h \rangle$ , and the mean dispersion,  $\sigma_h$ , of the hole volume as a function of temperature  $T$  for densified at 200 MPa (blue), gas-exposed (red) and untreated (black) COC and PC.

# $V_f$ vs $T(K)$



The specific free volume  $V_f = \langle v_h \rangle N_h'$  from PALS at  $10^{-5}$  Pa as a function of temperature for untreated (black filled circles), densified at 200 MPa (blue squares), and gas-exposed (read diamonds) COC and PC. The black empty circles show 0.1 MPa isobars from PVT experiments for the untreated polymers,  $V_f = hV$ .

Thanks for your time and patience!